

# Advanced Infosec Machine Model and DSLs



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John Launchbury

Thomas Nordin

Oregon Graduate Institute



# Overview of this talk

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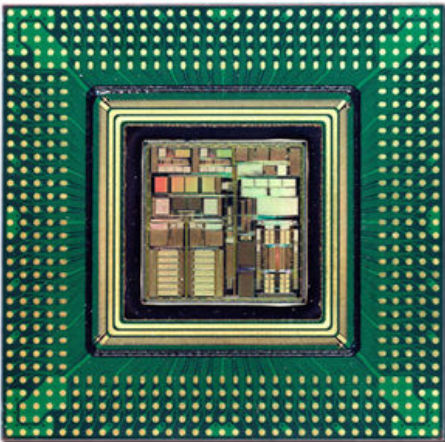
- AIM overview
- Introduction to OGI's AIM project
- Modeling permutations
  - Permutation building blocks
  - Building complex permutations from parts
- Modeling Sbox functions
- Summary



# AIM

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- Motorola AIM  
(Advanced INFOSEC Machine)



- On-board encryption engines
- MASK technology  
(Mathematically Assured Separation Kernel)
- Physically tamper-proof

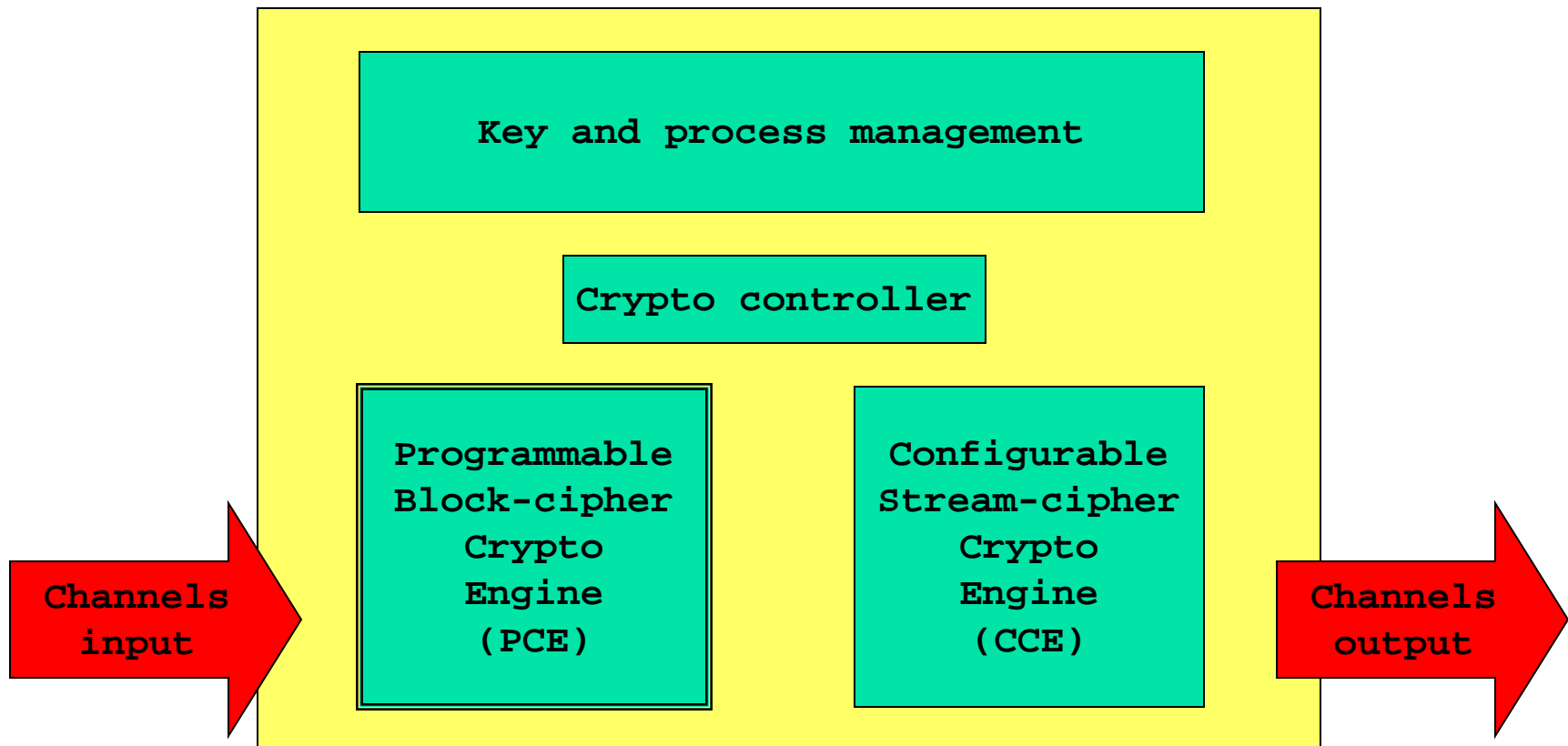


[www.motorola.com/GSS/SSTG/ISSPD/INFOSEC/Embedded/AIM/](http://www.motorola.com/GSS/SSTG/ISSPD/INFOSEC/Embedded/AIM/)



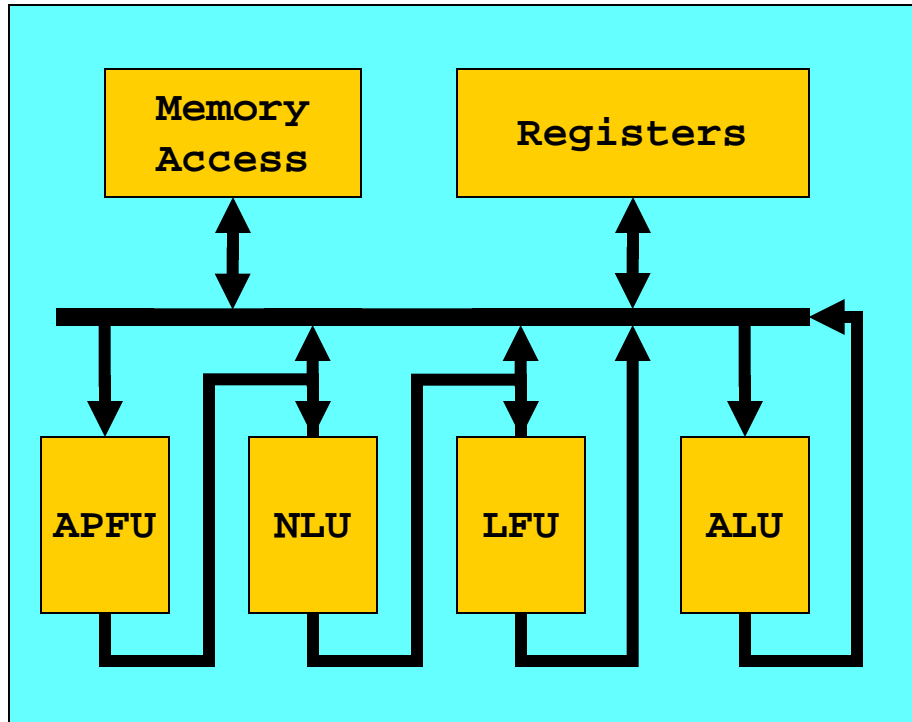
# AIM overview

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# (Simplified)

## PCE Internal Structure



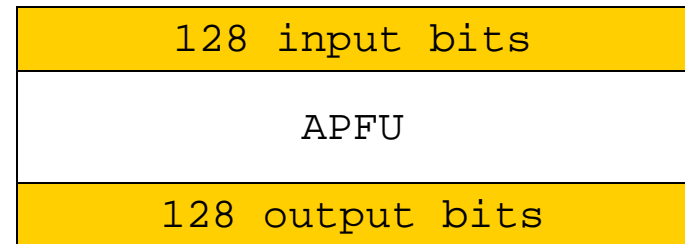
- Execution components
  - APFU (Permutation Function Unit)
    - 16 predefined permutations
  - NLU (Non-Linear Unit)
    - 16 one-bit memories
    - Independently addressable
  - LFU (Linear Function Unit)
    - XOR unit
  - ALU
- PCE microcode
  - Each component's in-parallel operation specified each cycle
  - Visible pipeline delays when accessing registers
  - Memory accessed via external requests



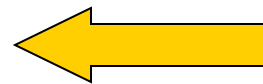
# OGI's Project

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- Semantic analysis of AIM microcode
  - How do the components of the AIM crypto-processor behave?
  - Does a piece of PCE microcode meet its specification? Where does it go wrong?
  - Automatic generation of AIM microcode

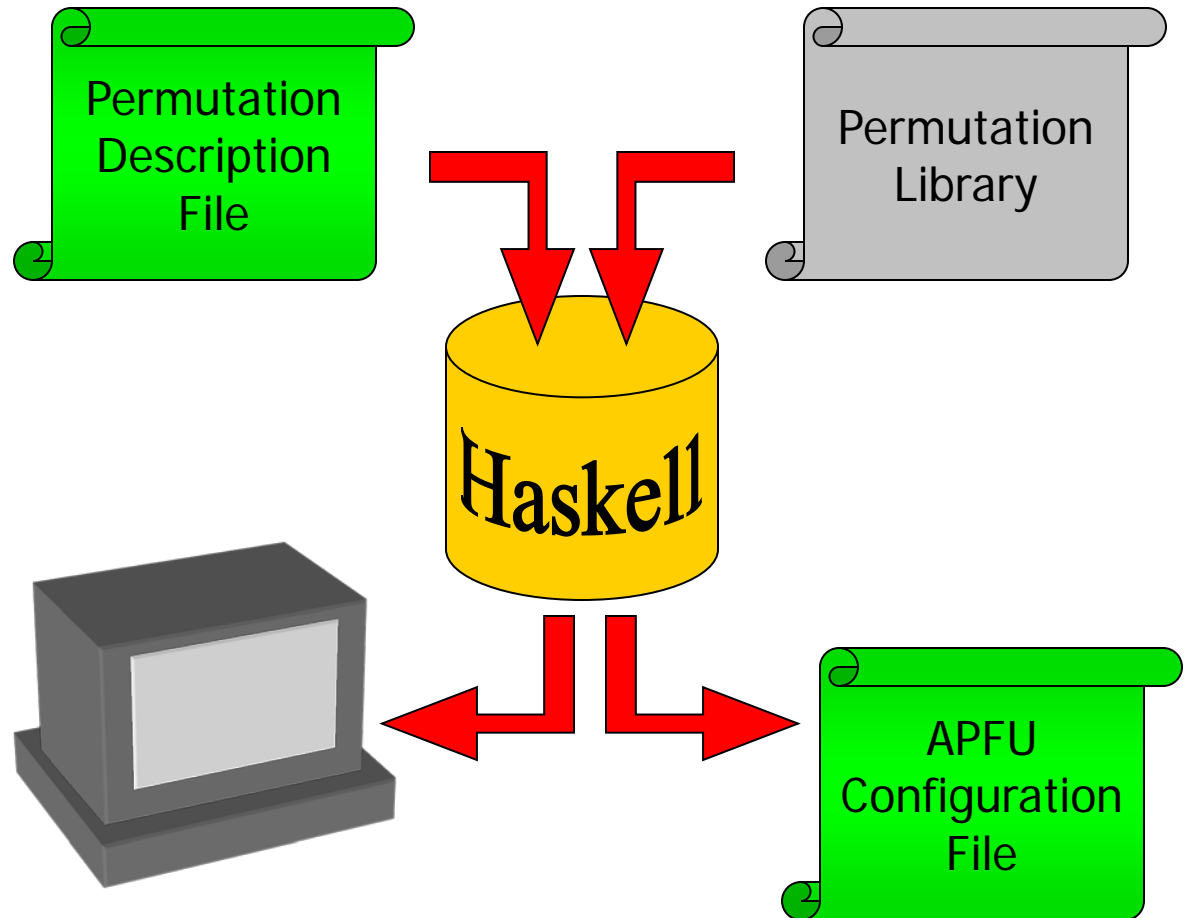


- In the process we have built the core of some potentially useful tools
  - Generating configuration files for permutation and Sbox specifications
  - AIM microcode single stepper



# Permutation Tool

- Permutations are described naturally
- Permutations can be explored to check they behave as predicted
- Permutations can be used to generate APFU configuration files



# Permutations

- Lists of numbers

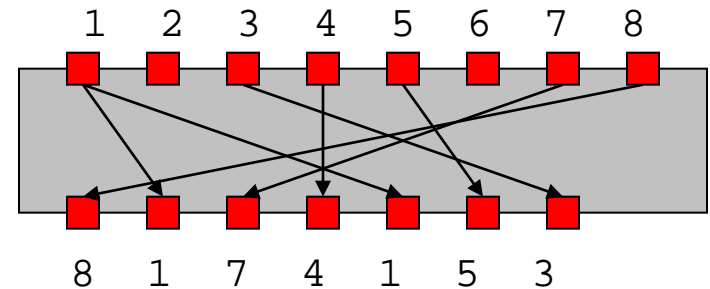
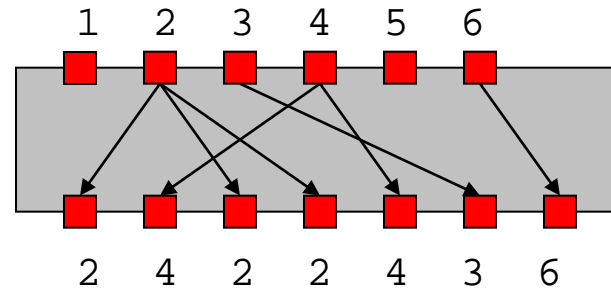
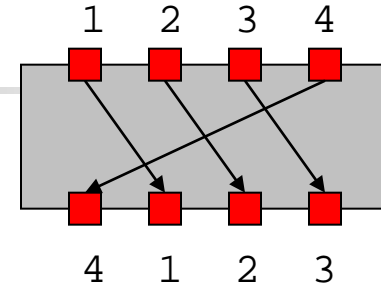
- Numbered left to right
- Beginning at 1

- Examples

- [4, 1, 2, 3]
- [2, 4, 2, 2, 4, 3, 6]
- [8, 1, 7, 4, 1, 5, 3]

- Permutations can be any size

- 16 or 32 bits is common







# List definitions

---

- At their simplest, permutations can be defined by just giving a list of bit positions
- Examples

desP =

```
[16, 7, 20, 21, 29, 12, 28, 17,  
 1, 15, 23, 26, 5, 18, 31, 10,  
 2, 8, 24, 14, 32, 27, 3, 9,  
 19, 13, 30, 6, 22, 11, 4, 25]
```

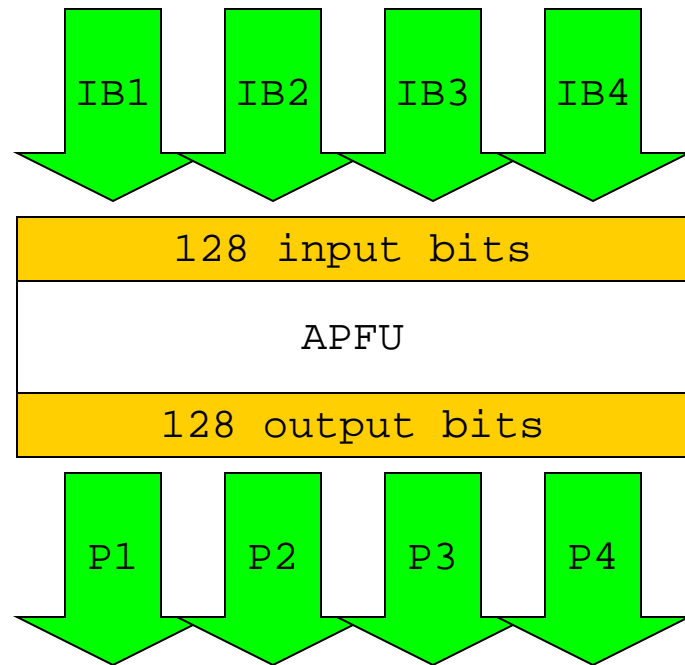
desIP =

```
[58, 50, 42, 34, 26, 18, 10, 2,  
 60, 52, 44, 36, 28, 20, 12, 4,  
 62, 54, 46, 38, 30, 22, 14, 6,  
 64, 56, 48, 40, 32, 24, 16, 8,  
 57, 49, 41, 33, 25, 17, 9, 1,  
 59, 51, 43, 35, 27, 19, 11, 3,  
 61, 53, 45, 37, 29, 21, 13, 5,  
 63, 55, 47, 39, 31, 23, 15, 7]
```

# AIM Input Permutations

- Input buffer permutations
  - Each selects the appropriate Permutation Unit input bits
    - Maps down to 32 output bits

```
ib1 = [1..32]
ib2 = [33..64]
ib3 = [65..96]
ib4 = [97..128]
```





# APFU definition

---

- APFU specification is a record containing
  - Permutation number
  - Four 32-bit permutations p1, p2, p3, p4
- Example

```
apfu5 = APFU {perm = 5,  
              p1 = ib4 `into` desP,  
              p2 = ib2,  
              p3 = ib3,  
              p4 = ib1}
```



# “Lego Block” Permutations

---

- Permutations are “values”
  - Like integers, complex numbers, polynomials, matrices etc.
  - Don’t think about storage
  - Think about operators
- Question
  - What operators are needed to produce new permutations from old?

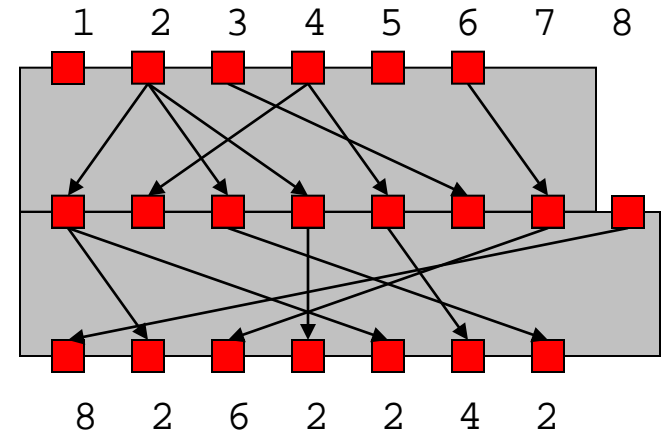
# `into`

- Pipe the output of one permutation into the input of another
- Calculate the resulting composite permutation
- Example

```
ib4 `into` desP
```

=

```
[112,103,116,117,125,108,124,113,  
 97,111,119,122,101,114,127,106,  
 98,104,120,110,128,123, 99,105,  
115,109,126,102,118,107,100,121]
```



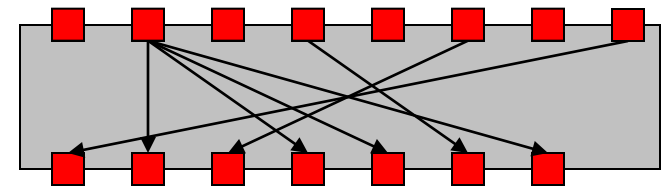
```
[2,4,2,2,4,3,6]
```

```
`into`
```

```
[8,1,7,4,1,5,3]
```

```
=
```

```
[8,2,6,2,2,4,2]
```



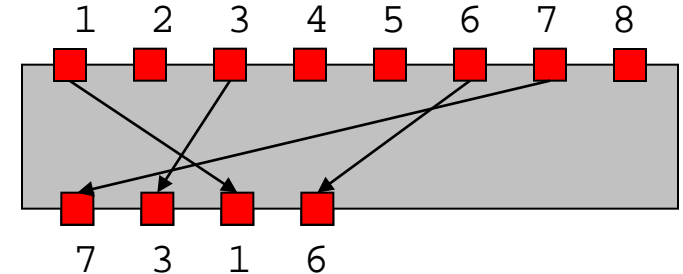
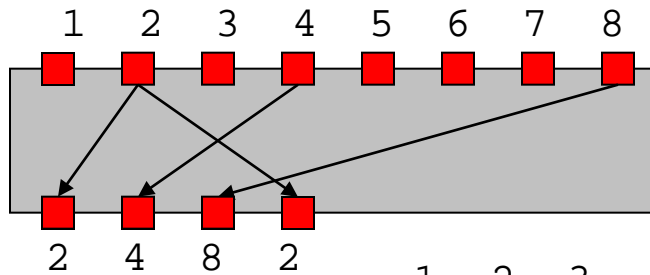
++

- Joins two permutations together, side by side
  - Each permutation draws from the same input bits
  - Obtained simply by appending the two lists together

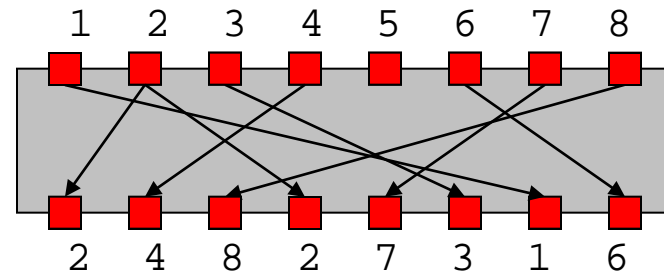
## ■ Example

ib4 ++ ib3

```
= [97, 98, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 110, 111, 112,
113, 114, 115, 116, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128,
65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80,
81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96]
```



$$[2, 4, 8, 2] ++ [7, 3, 1, 6] \\ = [2, 4, 8, 2, 7, 3, 1, 6]$$



# `select`

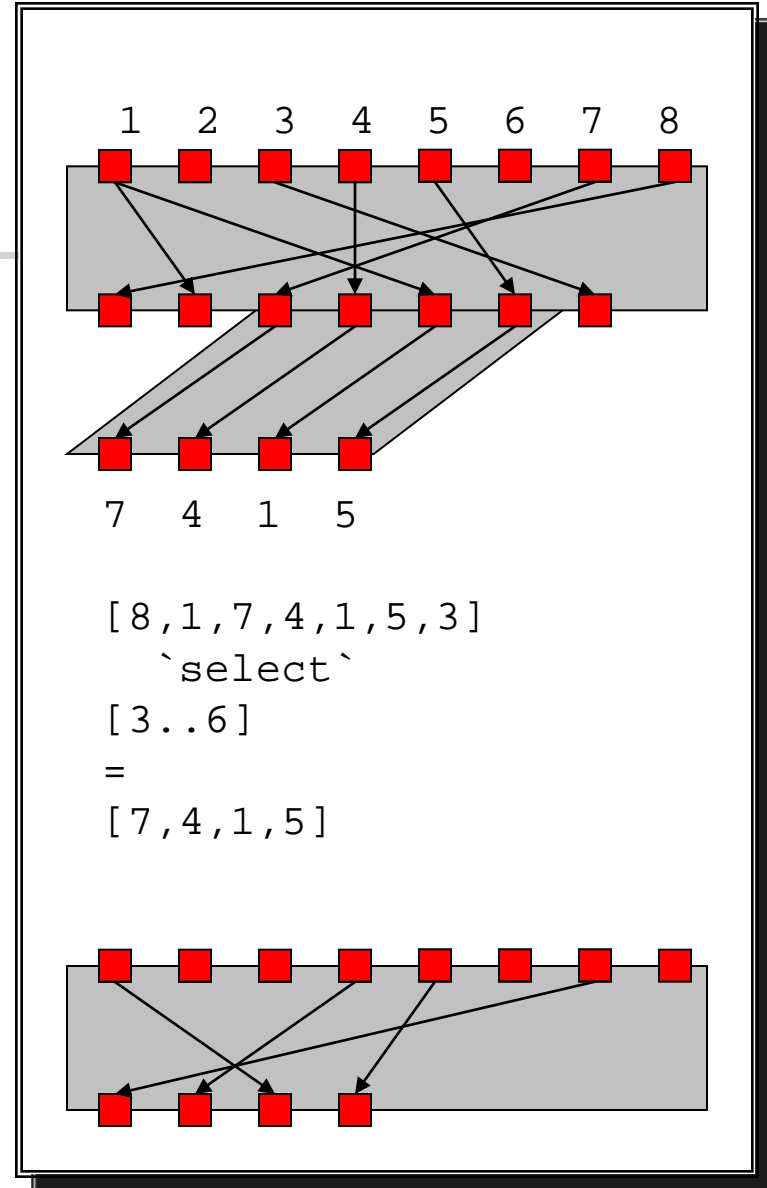
- Selects output bits from a permutation
  - Requires a list of contiguous output bits

## ■ Example

```
(ib3 ++ ib2) `select` [17..64]
```

=

```
[81,82,83,84,85,86,87,88,  
89,90,91,92,93,94,95,96,  
33,34,35,36,37,38,39,40,  
41,42,43,44,45,46,47,48,  
49,50,51,52,53,54,55,56,  
57,58,59,60,61,62,63,64]
```





<<<

- Left rotation of a permutation

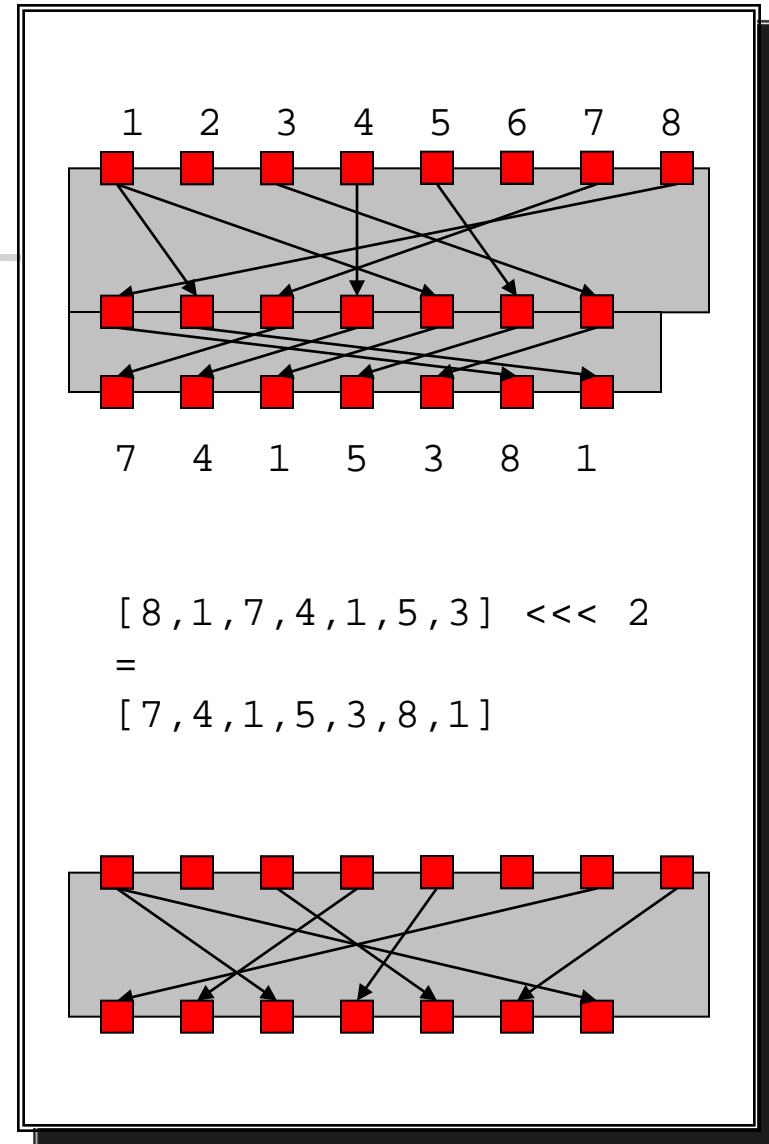
- Example

`[5..32] <<< 2`

`=`

`[ 7, 8, 9, 10, 11, 12, 13, 14,  
15, 16, 17, 18, 19, 20, 21, 22,  
23, 24, 25, 26, 27, 28, 29, 30,  
31, 32, 5, 6]`

- Right rotation (`>>>`) is the converse





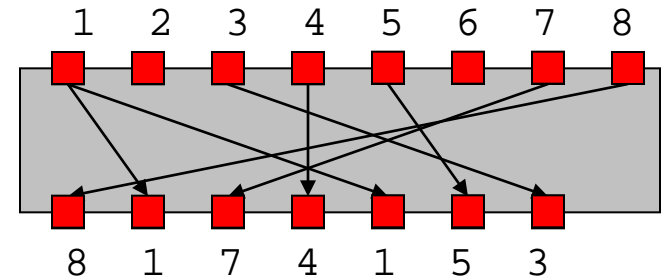
# inverse

- Invert a permutation
- Example

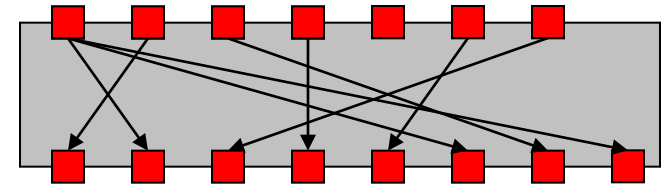
`inverse desIP`

```
= [40,8,48,16,56,24,64,32,  
   39,7,47,15,55,23,63,31,  
   38,6,46,14,54,22,62,30,  
   37,5,45,13,53,21,61,29,  
   36,4,44,12,52,20,60,28,  
   35,3,43,11,51,19,59,27,  
   34,2,42,10,50,18,58,26,  
   33,1,41, 9,49,17,57,25]
```

- If  $p$  is a true permutation (no duplication, no losses) then
  - $\text{inverse } p \text{ into } p = \text{id} = p \text{ into } \text{inverse } p$



```
inverse [8,1,7,4,1,5,3]  
=  
[2,1,7,4,6,1,3,1]
```



# pad

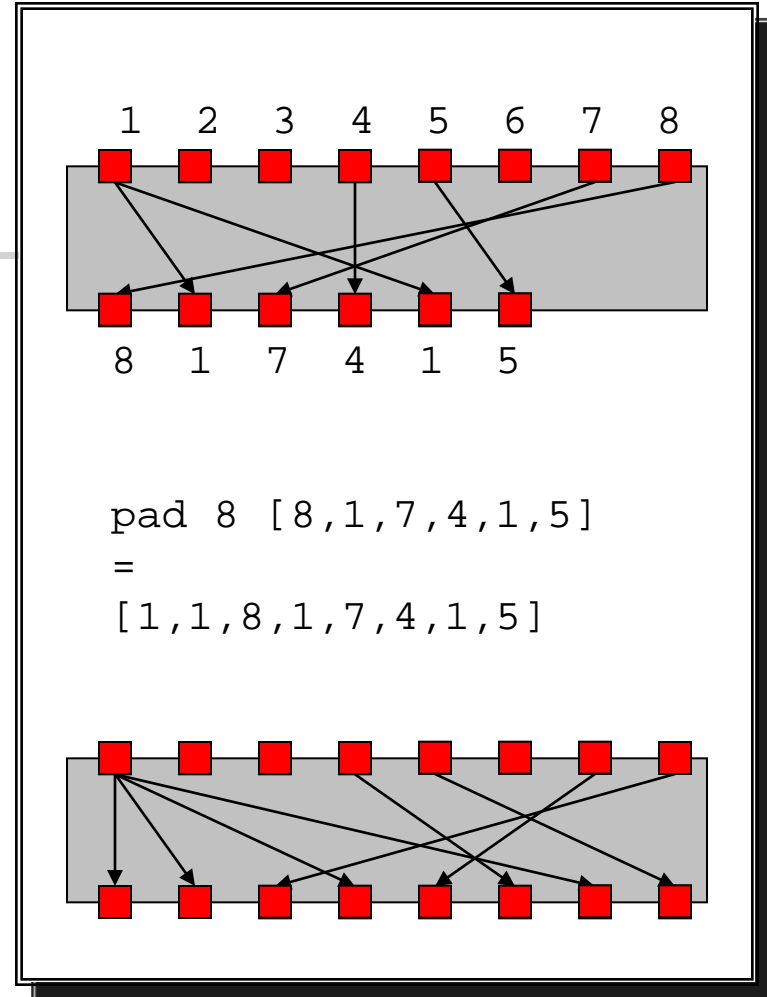
- Pad the output of a permutation to make its output the desired width

- Example

```
pad 32 ([5..32] <<< 1)
= [ 1, 1, 1, 1, 6, 7, 8, 9,
    10,11,12,13,14,15,16,17,
    18,19,20,21,22,23,24,25,
    26,27,28,29,30,31,32, 5]
```

- NB. It is an error to pad less than the size of the permutation

- `pad 4 [1,2,3,4,5] --> Error`





# Example Definitions

---

```
apfu1 = APFU {perm = 1,  
              p1 = pad 32 (expansion `select` [1..16]),  
              p2 = expansion `select` [17..48],  
              p3 = ib1,  
              p4 = initialPerm `select` [33..64]}
```

where

```
initialPerm = (ib3 ++ ib4) `into` desIP  
expansion = (initialPerm `select` [33..64]) `into` desE
```

```
desE = [32, 1, 2, 3, 4, 5, 4, 5, 6, 7, 8, 9  
        , 8, 9, 10, 11, 12, 13, 12, 13, 14, 15, 16, 17  
        , 16, 17, 18, 19, 20, 21, 20, 21, 22, 23, 24, 25  
        , 24, 25, 26, 27, 28, 29, 28, 29, 30, 31, 32, 1 ]
```



# "Value" of APFU1

---

```
DES> apful
```

```
APFU{perm=1,  
    p1=[1,1,1,1,1,1,1,1,1,1,1,1,1,1,1,  
        71,121,113,105,97,89,97,89,81,73,65,123,65,123,115,107],  
    p2=[99,91,99,91,83,75,67,125,67,125,117,109,101,93,101,93,  
        85,77,69,127,69,127,119,111,103,95,103,95,87,79,71,121],  
    p3=[1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,  
        17,18,19,20,21,22,23,24,25,26,27,28,29,30,31,32],  
    p4=[121,113,105,97,89,81,73,65,123,115,107,99,91,83,75,67,  
        125,117,109,101,93,85,77,69,127,119,111,103,95,87,79,71]  
}
```

# Displaying APFUs

NB. All indices have been automatically converted to be AIM compliant (numbered right to left, starting at 0)

```
Main> viewCode apfu5
```

```
PERM5:
```

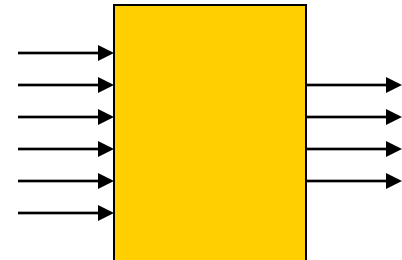
```
P1_31(IB4_16) | P2_31(IB2_31) | P3_31(IB3_31) | P4_31(IB1_31) |
P1_30(IB4_25) | P2_30(IB2_30) | P3_30(IB3_30) | P4_30(IB1_30) |
P1_29(IB4_12) | P2_29(IB2_29) | P3_29(IB3_29) | P4_29(IB1_29) |
P1_28(IB4_11) | P2_28(IB2_28) | P3_28(IB3_28) | P4_28(IB1_28) |
P1_27(IB4_3) | P2_27(IB2_27) | P3_27(IB3_27) | P4_27(IB1_27) |
P1_26(IB4_20) | P2_26(IB2_26) | P3_26(IB3_26) | P4_26(IB1_26) |
P1_25(IB4_4) | P2_25(IB2_25) | P3_25(IB3_25) | P4_25(IB1_25) |
P1_24(IB4_15) | P2_24(IB2_24) | P3_24(IB3_24) | P4_24(IB1_24) |
P1_23(IB4_31) | P2_23(IB2_23) | P3_23(IB3_23) | P4_23(IB1_23) |
P1_22(IB4_17) | P2_22(IB2_22) | P3_22(IB3_22) | P4_22(IB1_22) |
P1_21(IB4_9) | P2_21(IB2_21) | P3_21(IB3_21) | P4_21(IB1_21) |
P1_20(IB4_6) | P2_20(IB2_20) | P3_20(IB3_20) | P4_20(IB1_20) |
:
:
P1_2(IB4_21) | P2_2(IB2_2) | P3_2(IB3_2) | P4_2(IB1_2) |
P1_1(IB4_28) | P2_1(IB2_1) | P3_1(IB3_1) | P4_1(IB1_1) |
P1_0(IB4_7) | P2_0(IB2_0) | P3_0(IB3_0) | P4_0(IB1_0);
```



# S-boxes

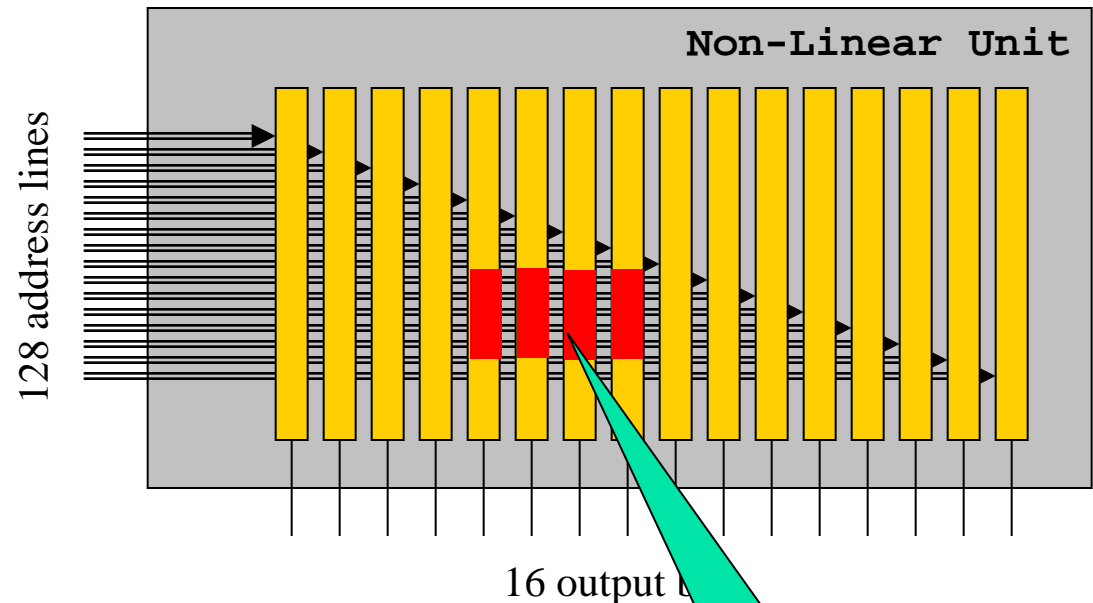
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- Every crypto-algorithm needs non-linear components
  - Multiplication (RC6)
  - Galois field inversion (Rijndael)
  - Arbitrary functions, S-boxes
    - DES has 8 separate S-boxes
    - Each 6-bit in, 4-bit out



# Implementing S-boxes

- NLU designed for S-box functionality
- Lookup tables allow arbitrary functions
  - Sixteen 256x1 tables
  - Each table independently addressable
  - Permutations used for arranging address lines
  - Examples
    - 256 x 16-bit words
    - 512 bytes, dual read ports

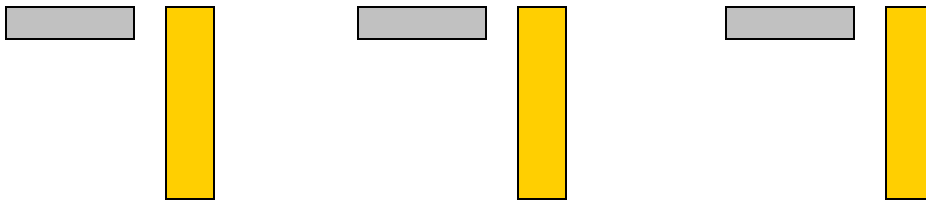


single  
6->4  
S-box

# Modeling S-boxes

- Underlying model

- Sequence of permutation/bit-list pairs



Permutation selects  
address lines for  
indexing its bit-  
list

Bit-list entries.  
 $|\text{bit-list}| =$   
 $2 \wedge |\text{perm}|$

- Component permutations will be joined to build the final addressing permutation
  - Component bit-lists will be joined to construct the values of each look-up table
- What are the compositional operations?
    - Primitive construction of a single S-box from a list of values
    - Joining S-boxes together side-by-side, or vertically
    - Rearranging addressing lines
    - Computing new S-boxes from old





# Operators

---

- Build a primitive S-box given an addressing permutation, the number of output bits, and a table of data

`sbox :: Perm -> Int -> [Integer] -> Sbox`

- Connect multiple S-boxes together vertically, given an addressing permutation which distinguishes which S-box is required

`pack :: Perm -> [Sbox] -> Sbox`

- Connect multiple S-boxes together horizontally

`extend :: [Sbox] -> Sbox`

- Pre-compose a new addressing permutation with the S-box permutations

`intoS :: Perm -> Sbox -> Sbox`



# Example definitions

---

```
sbox1 = pack [1,6] [sbox1a, sbox1b, sbox1c, sbox1d]
```

```
sbox1a = sbox [2,3,4,5] 4  
         [14,4,13,1,2,15,11,8,3,10,6,12,5,9,0,7]
```

```
sbox1b = sbox [2,3,4,5] 4  
         [0,15,7,4,14,2,13,1,10,6,12,11,9,5,3,8]
```

```
sbox1c = sbox [2,3,4,5] 4  
         [4,1,14,8,13,6,2,11,15,12,9,7,3,10,5,0]
```

```
sbox1d = sbox [2,3,4,5] 4  
         [15,12,8,2,4,9,1,7,5,11,3,14,10,0,6,13]
```



# Introducing a little abstraction

---

```
desBox xss = pack [1,6] (map (sbox [2,3,4,5] 4) xss)
```

```
sbox4 = desBox
```

```
  [[7,13,14,3,0,6,9,10,1,2,8,5,11,12,4,15]  
   ,[13,8,11,5,6,15,0,3,4,7,2,12,1,10,14,9]  
   ,[10,6,9,0,12,11,7,13,15,1,3,14,5,2,8,4]  
   ,[3,15,0,6,10,1,13,8,9,4,5,11,12,7,2,14]  
  ]
```



# Packing the table

---

```
layer1 = extend [
                [9..14] `into` sbox1,
                [17..22] `into` sbox2,
                [25..30] `into` sbox3]
```

```
layer2 = extend [
                [9..14] `into` sbox4,
                [17..22] `into` sbox5,
                [25..30] `into` sbox6]
```

```
allDES = pack [7] [layer1, layer2]
```



# Generating AIM configurations

- All the information can be calculated for the AIM configuration file
  - Format requires rearranging NLU data as 16-bit words
- Use the `viewSbox` command

```
> viewSbox allDES
NLF_BLOCK:
F0(0xefa7) |
F1(0x410d) |
F2(0xd89e) |
F3(0x1ee3) |
F4(0x2660) |
:
F124(0xa6e3) |
F125(0x4025) |
F126(0x5836) |
F127(0x3dcb) ;
```



# Laws

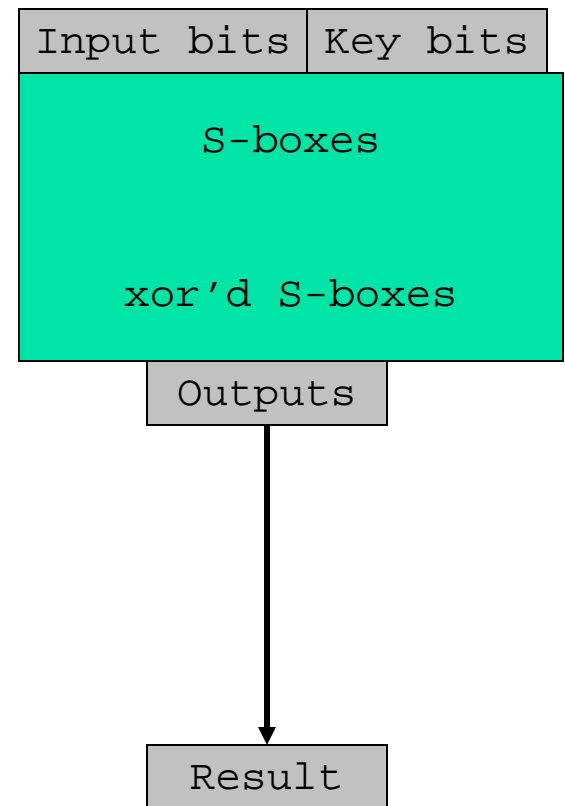
---

- Formal basis means that we should look for natural algebraic laws
  - Helps provide understanding of the operators
- Pre-composition law

$$p \text{ `intoS` } (sbox \ q \ n \ xs)$$
$$=$$
$$sbox \ (p \text{ `into` } \ q) \ n \ xs$$

# Exploiting the power

- DES S-boxes only require half NLU tables
  - What should the rest of the space be used for?
- Usually, table filled out with duplication
- Instead, pre-compute xor with key material





# Summary

---

- Formal modeling
  - Family of operators for building permutations and S-boxes
  - Formal semantics for the operators
  - Commands for generating AIM configuration files
- Lessons
  - Separation of model from display
  - Power of little domain-specific languages
    - Made cheap by embedding in clean host language