Rule Based Systems and the Intersection of Formal Methods and Testing Rick Kuhn, Vincent Hu, David Ferraiolo, Raghu Kacker, Dylan Yaga, and Yu Lei*

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Pseudo-exhaustive testing solution using covering arrays:

- determine dependencies
- partition according to these dependencies
- exhaustively test the inputs on which an output is dependent
- for access control:
 - convert rule antecedents to k-DNF form, producing sets of k or fewer attributes that will produce a "grant" decision
 - generate separate k-way covering arrays for combinations that should produce "grant" and "deny"

COMPARISON

0 1 0 0 1 1 1 grant for each set of inputs

determine expected decision

generate covering arrays with constraint from rules

array -

covering array deny

Positive Testing (The Easy Part)

- want to ensure that any set of appropriate attributes produces grant decision
- test set Gtest: every test should produce a response of grant.
- for any input where some combination of k input values matches a grant condition, a decision of grant is returned.
- Construct test set Gtest with one test for each term of *R* as follows:
- Gtest_i = $T_i \bigwedge -T_j$
- one test for each term in access control rule antecedents, with constraint removing any combination that would mask a fault
- example: testing that ab results in grant, for ab + cd \rightarrow grant, enforce constraint \sim (cd)

Example: Why It Works

- rule structure:
 - $R_1 \rightarrow \text{grant}$ \rightarrow grant R_2
 - • •
 - \rightarrow grant else \rightarrow deny

| | a | b | С | d | е |
|-----|---|---|---|---|---|
| 1 | 0 | 0 | 0 | 0 | 0 |
| 2 | 0 | 0 | 1 | 1 | 1 |
| 3 | 0 | 1 | 1 | 0 | 0 |
| 4 | 1 | 0 | 0 | 1 | 0 |
| 5 | 1 | 0 | 1 | 1 | 0 |
| 6 | 1 | 1 | 0 | 0 | 1 |
| 7 | 1 | 1 | 1 | 1 | 1 |
| 8 | 0 | 0 | 1 | 0 | 1 |
| 9 | 1 | 1 | 0 | 1 | 0 |
| 10 | 0 | 0 | 0 | 1 | 1 |
| 11 | 1 | 0 | 0 | 0 | 0 |
| 12 | 0 | 1 | 1 | 1 | 0 |
| 13 | 1 | 0 | 0 | 0 | 1 |
| 14_ | 0 | 1 | 1 | 0 | 1 |

covering array containing all t-way tuples except for those in a grant condition

Number of Tests

- \bullet
- \bullet



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Negative Testing (The Hard Part)

• test set Dtest = covering array of strength k, for the set of attributes included in R

• constraints specified by $\sim R$

 ensures that all deny-producing conjunctions of attributes tested

• masking is not a consideration – because of problem structure

- deny is issued only after all grant conditions have been evaluated

 masking of one combination by another can only occur for Dtest when a test produces a response of grant

- if so, an error has been discovered; repair and run test set again

for positive tests, Gtest: one test for each term in the rule set, for for m rules with p terms each , mp for negative tests, Dtest: one covering array per rule, where each attribute in the rule is a factor

| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$ | 720 1800 900 2250 6120 15300 7540 |
|--|---|
| $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | 1800 900 2250 6120 15300 7540 |
| $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | 900 2250 6120 15300 7540 |
| 4 50 50 200 4 50 20 306 80 50 20 200 100 20 378 80 | 2250 6120 15300 7540 |
| 4 50 20 306 80 50 200 100 20 378 80 | 6120 15300 7540 |
| 50 200 100 20 378 80 | 15300 |
| 100 20 378 80 | 7540 |
| | / 500 |
| 50 200 | 18900 |
| 6 50 20 1041 80 | 20820 |
| 50 200 | 52050 |
| 100 20 1298 80 | 25960 |
| 50 200 | 64900 |
| 2 50 20 98 80 | 1960 |
| 50 200 | 4900 |
| 100 20 125 80 | 2500 |
| 50 200 | 6250 |
| 4 50 20 1821 80 | 36420 |
| 50 200 | 91050 |
| 100 20 2337 80 | 46740 |
| 50 200 1 | 16850 |
| 6 50 20 9393 80 1 | 87860 |
| 50 200 4 | 69650 |
| 100 20 12085 80 2 | 41700 |
| 50 200 6 | 04250 |