



# Privacy & Security in Machine Learning / Optimization

Nitin Vaidya

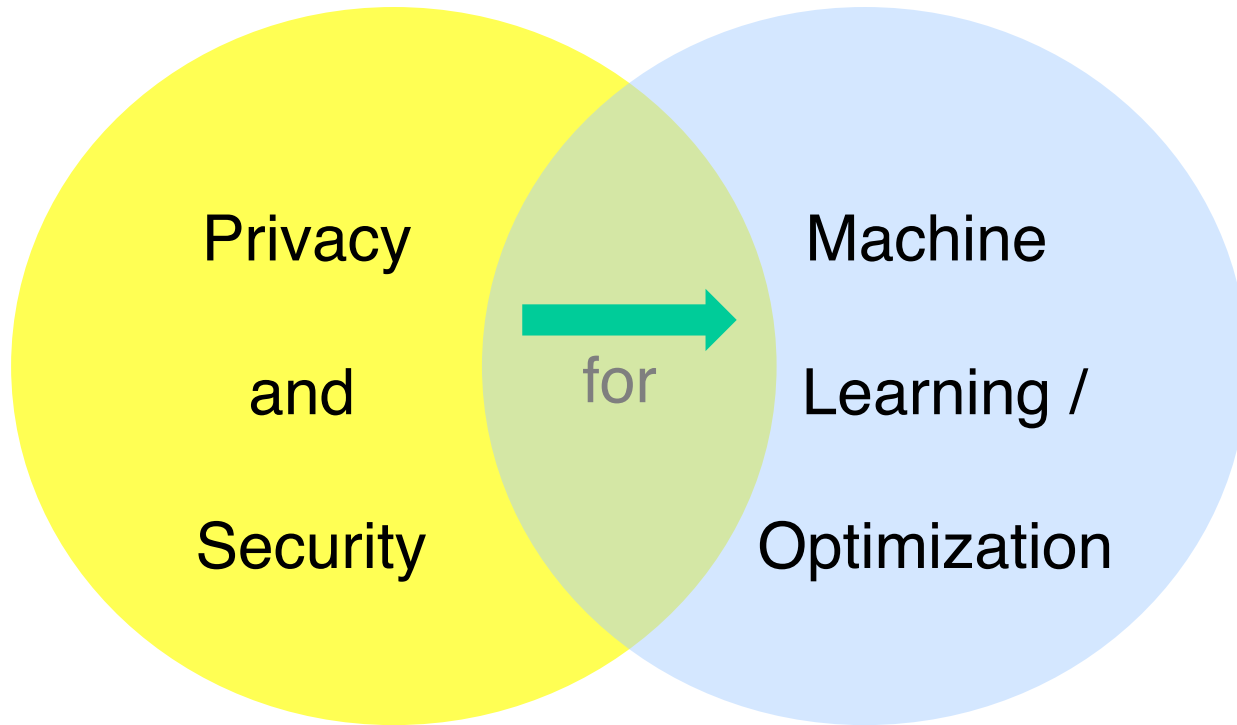
University of Illinois at Urbana-Champaign

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# Research Interests

## Distributed algorithms

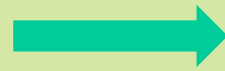
- Distributed shared memory systems
- Distributed computations over wireless networks
- Distributed optimization



Privacy

and

Security

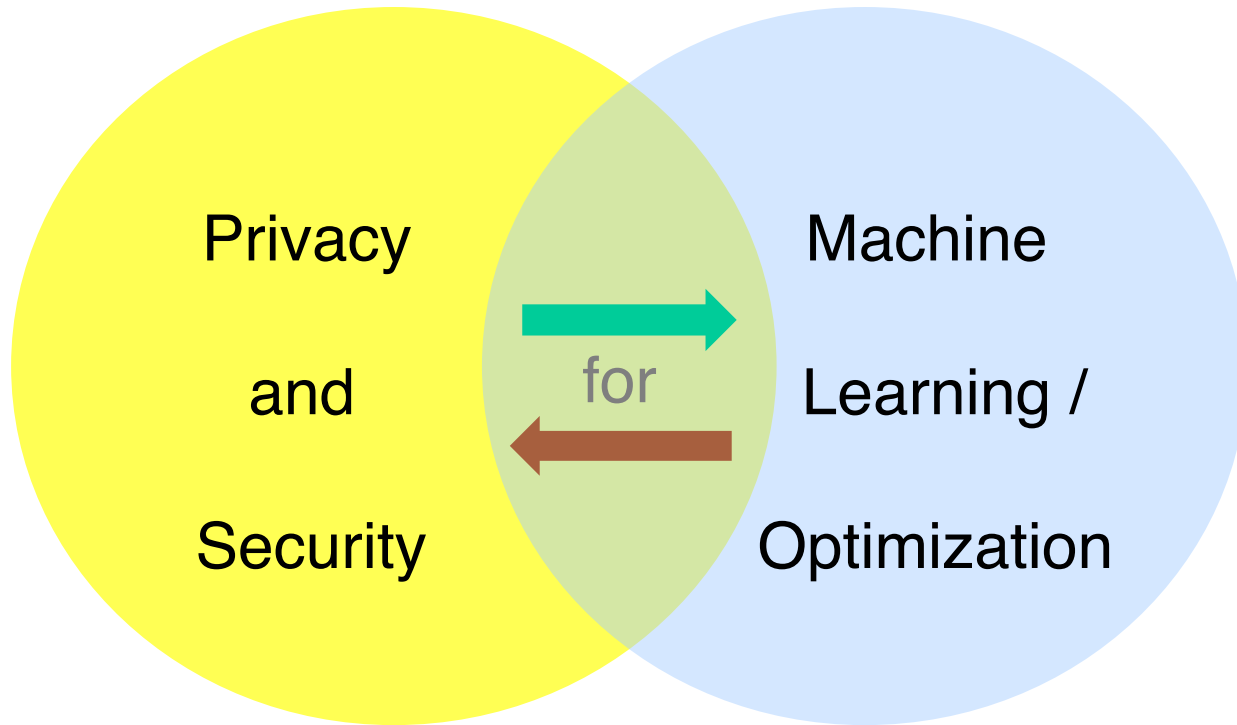


for

Machine

Learning /

Optimization

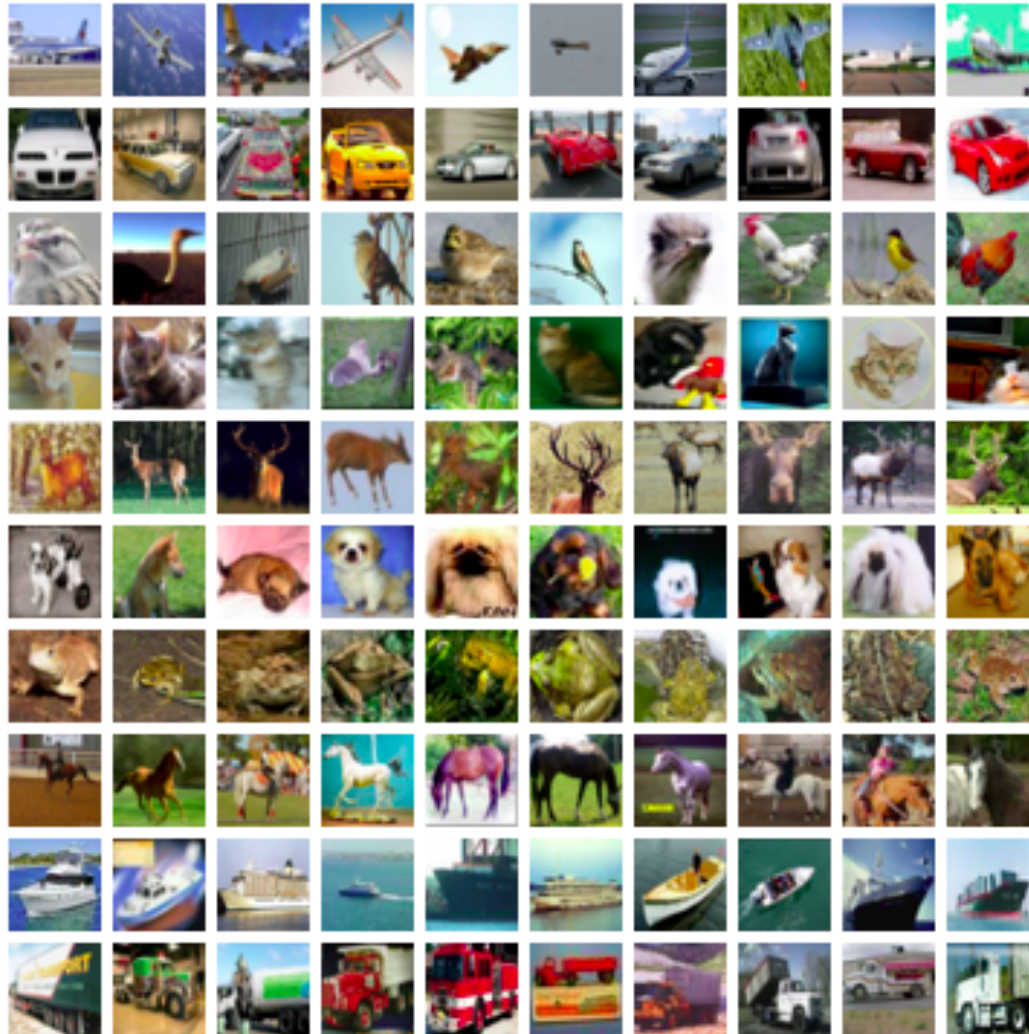


# Outline

- Motivation – distributed machine learning
- Research problems
  - Privacy-preserving distributed optimization
  - Adversarial learning
  - Robustness to adversarial samples



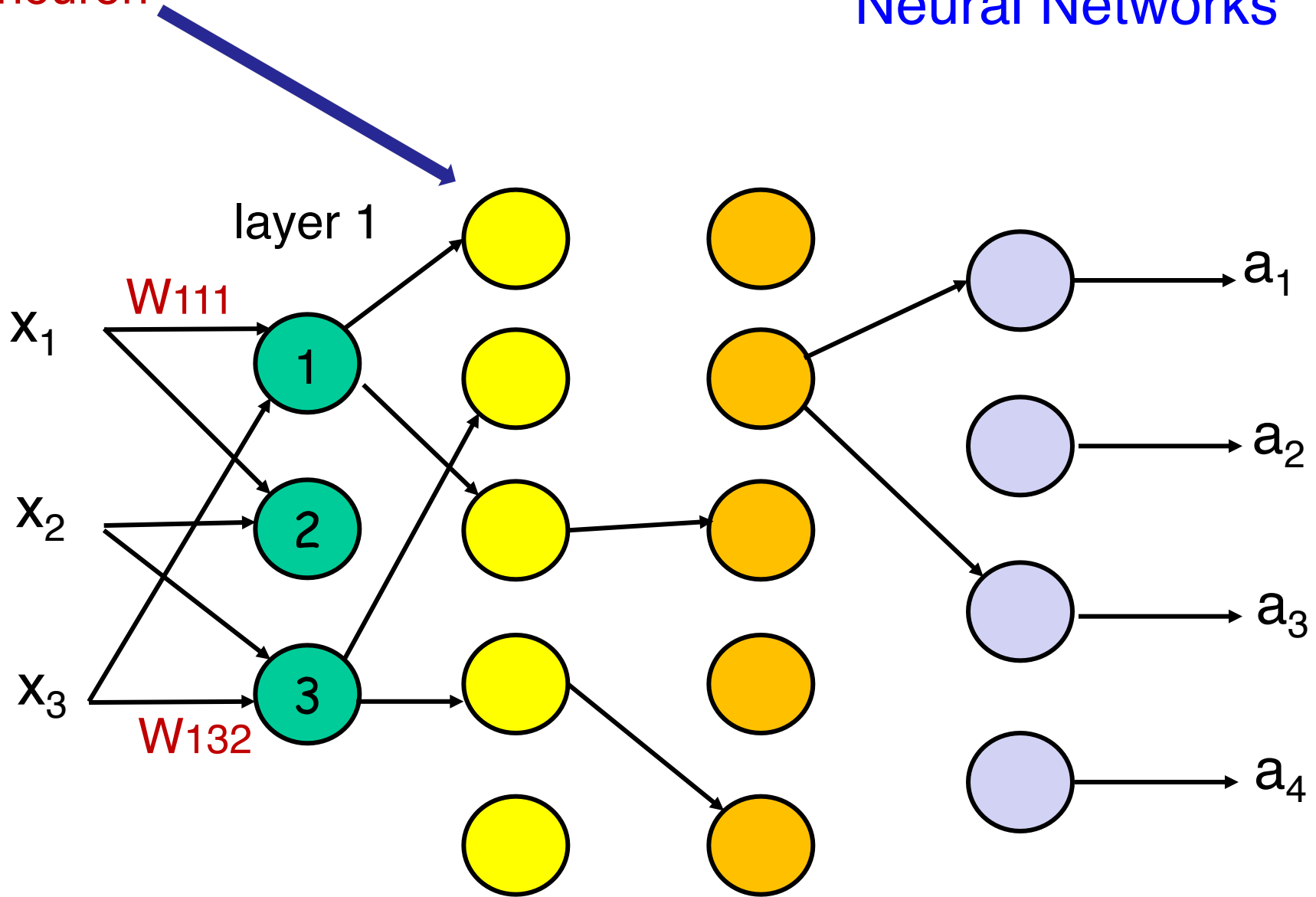
# Example – Image Classification



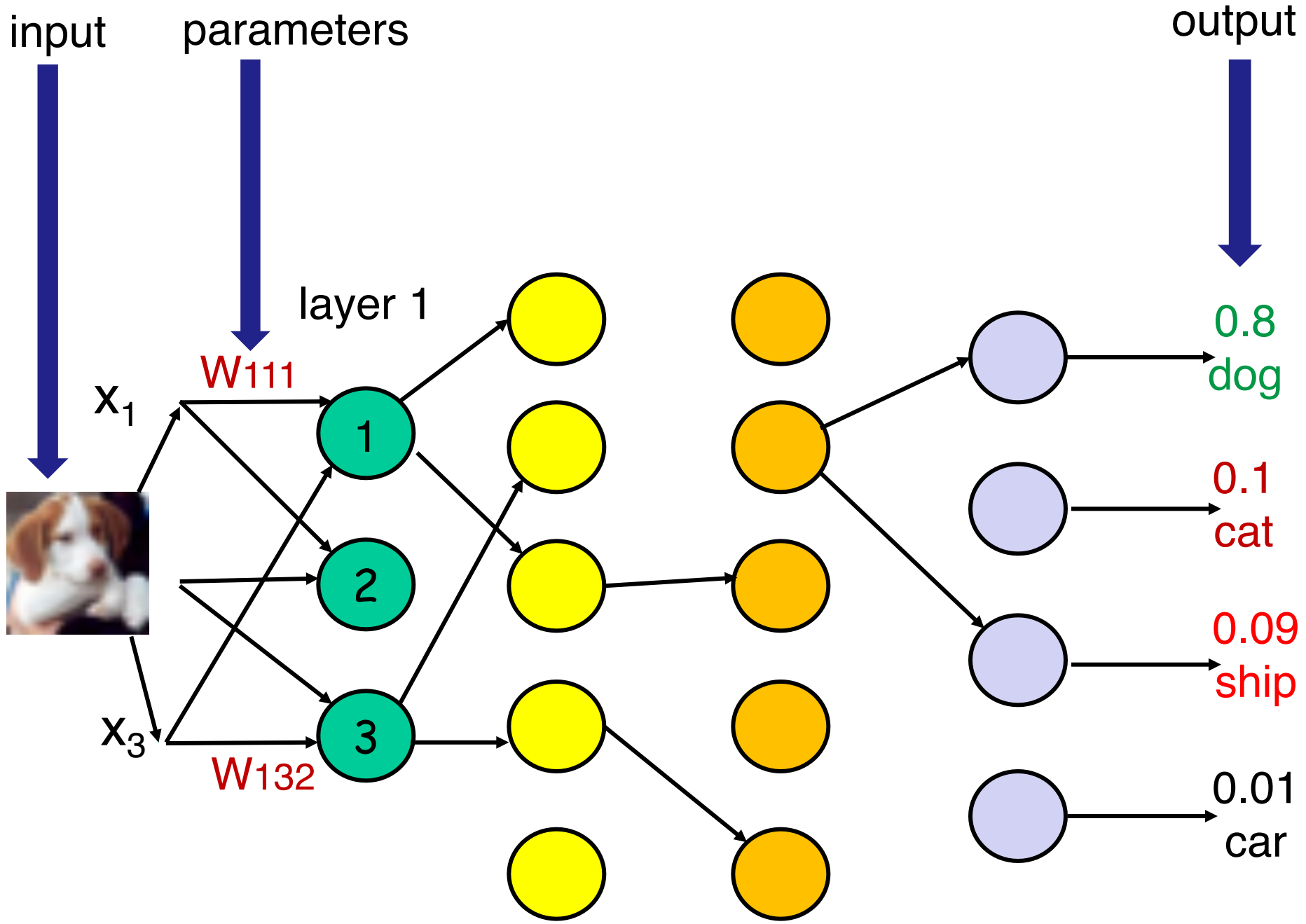
CIFAR-10  
dataset

# Deep Neural Networks

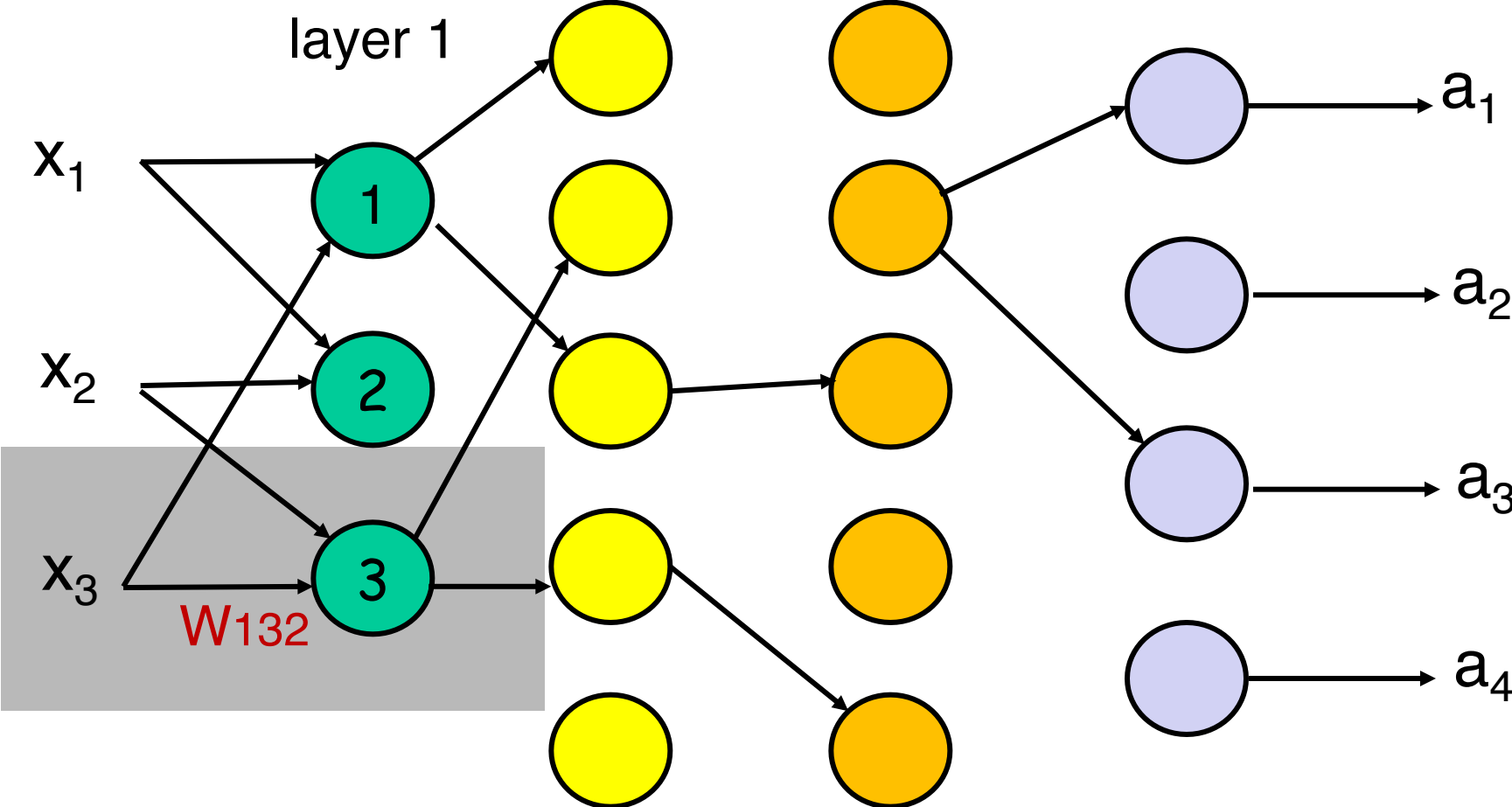
neuron

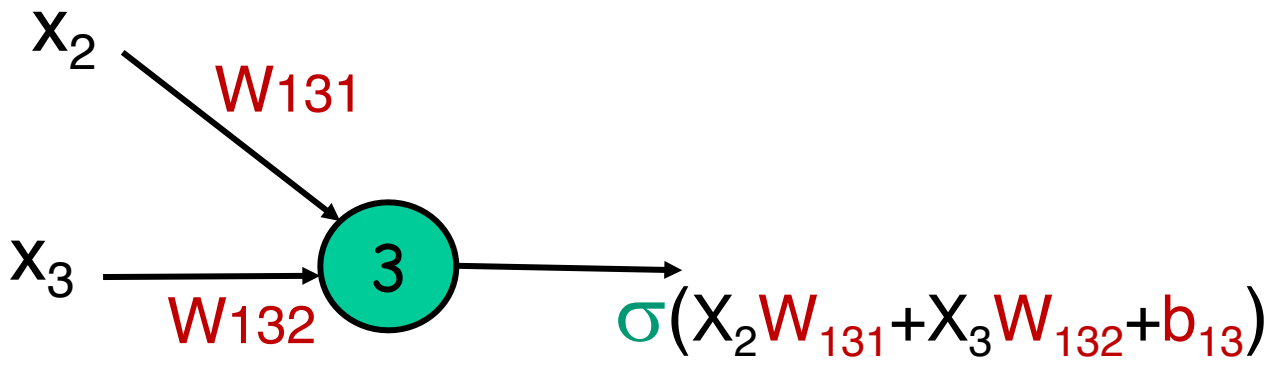


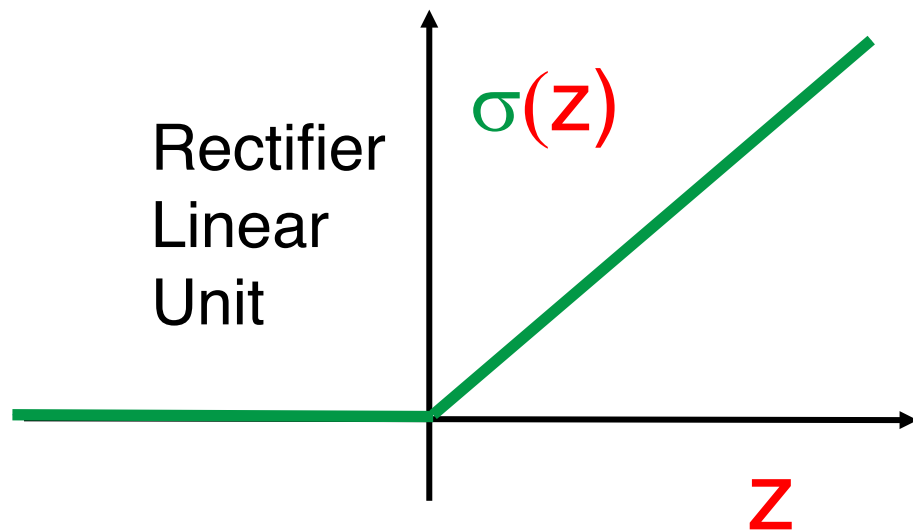
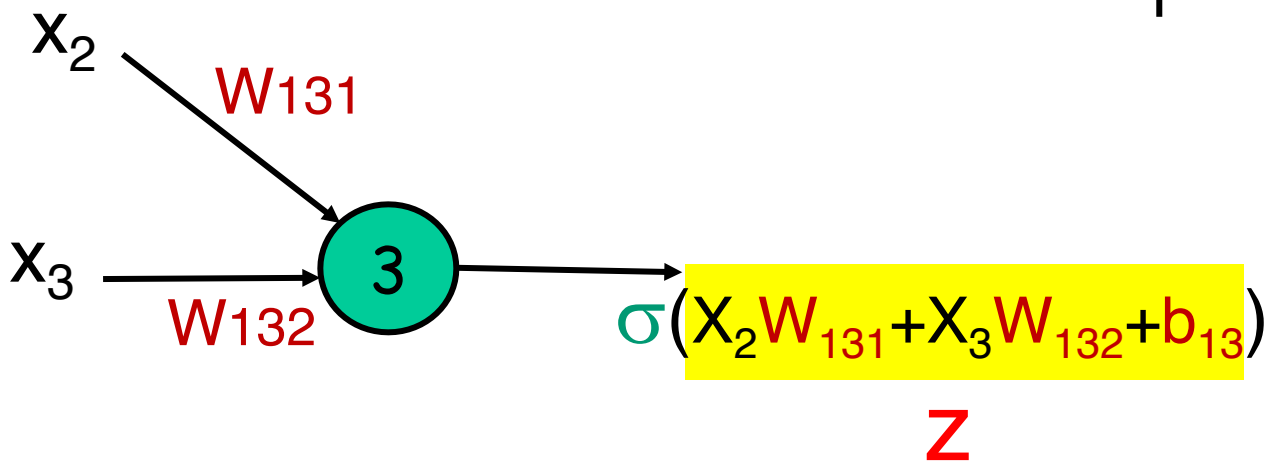




# Deep Neural Networks







# How to train your ~~dragon~~ network

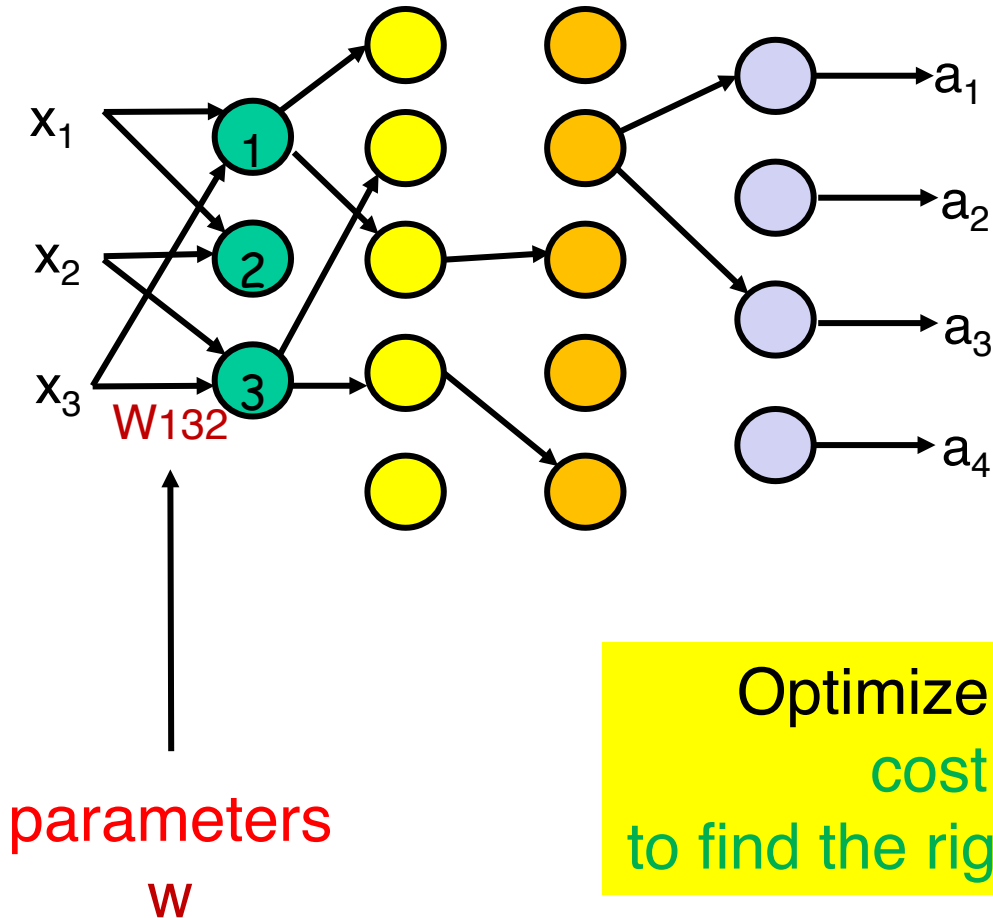
- Given a machine structure
- Parameters are the only free variables
- Choose parameters that maximize accuracy

# How to train your network

- Given a machine structure
  - Parameters are the only free variables
- Choose parameters to maximize accuracy

Optimize a suitably defined  
cost function  $h(w)$   
to find the right parameter vector  $w$

# How to train your network



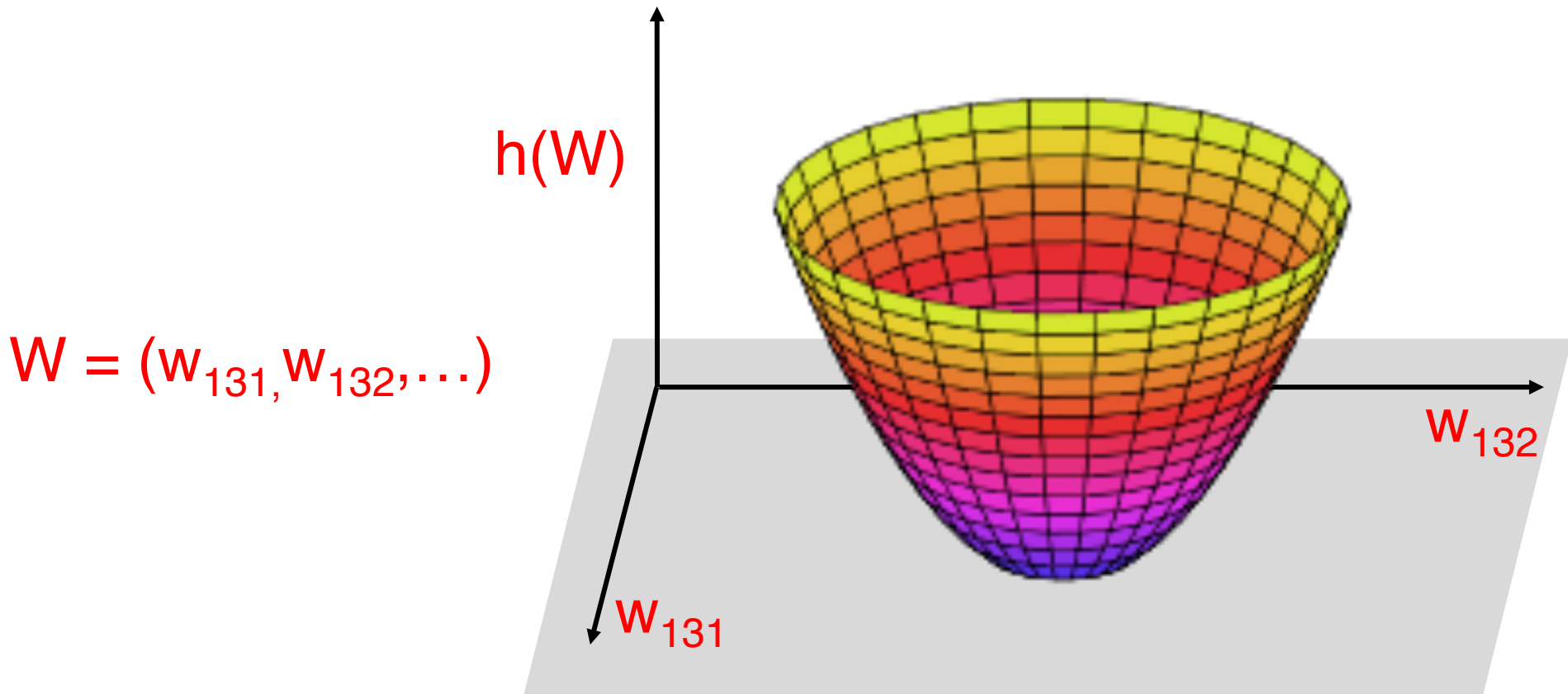
Optimize a suitably defined  
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to find the right parameter vector  $w$

## Cost Function $h(w)$

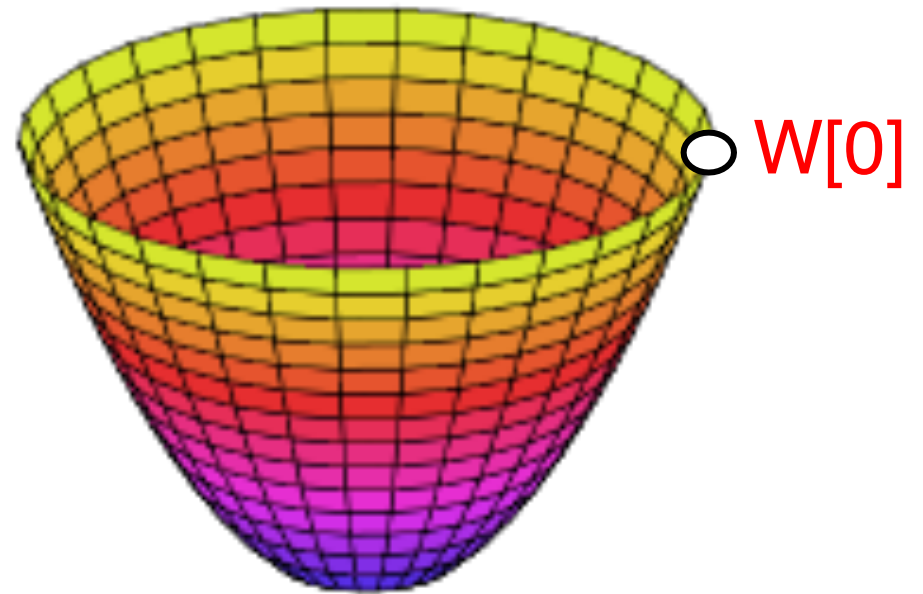
- Consider input  $x$
- True classification  $y(x)$
- Machine classification  $a(x,w)$  using parameters  $w$
- Cost for input  $x = \| y(x) - a(x,w) \|^2$
- Total cost  $h(w) = \sum_x \| y(x) - a(x,w) \|^2$



# Convex Optimization



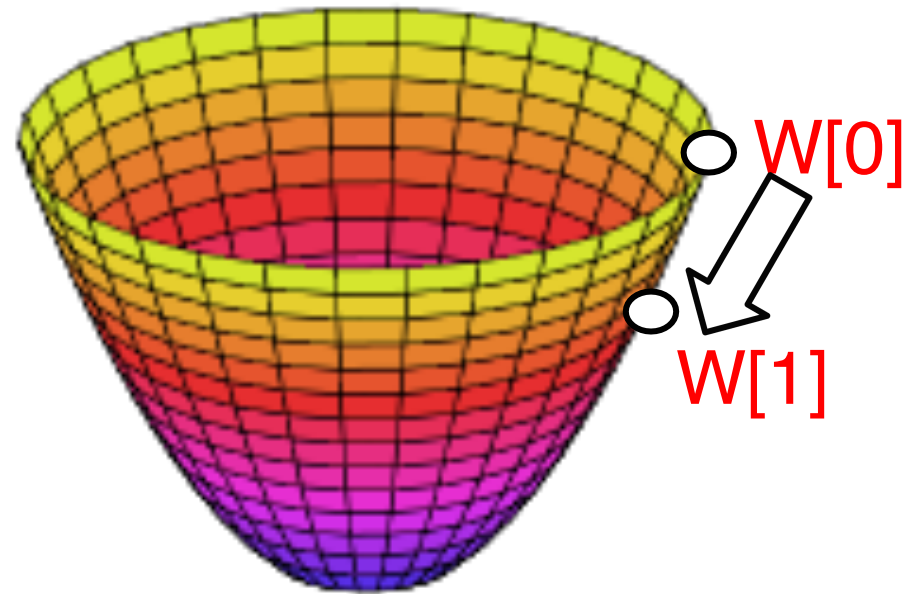
# Convex Optimization



$$W = (w_{131}, w_{132}, \dots)$$

$$W[0] = (4, 3, \dots)$$

# Convex Optimization

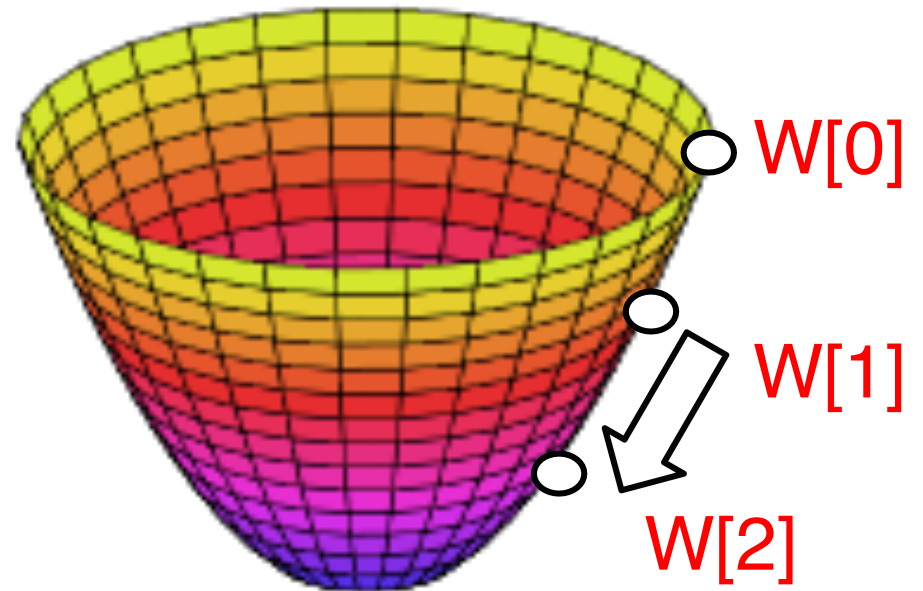


$$W = (w_{131}, w_{132}, \dots)$$

$$W[0] = (4, 3, \dots)$$

$$W[1] = (3, 2, \dots)$$

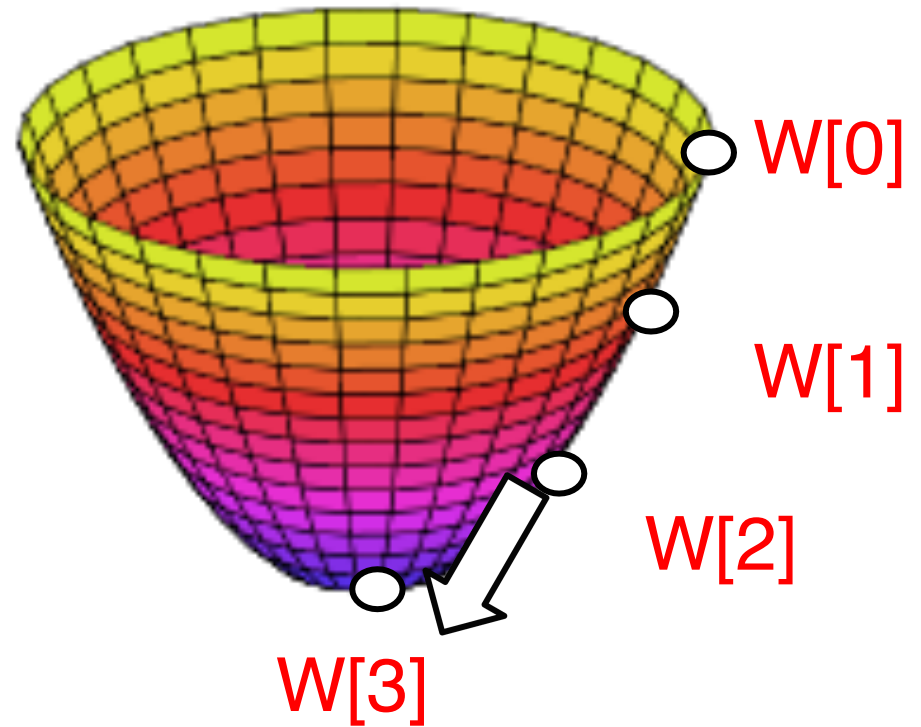
# Convex Optimization



$$W = (w_{131}, w_{132}, \dots)$$

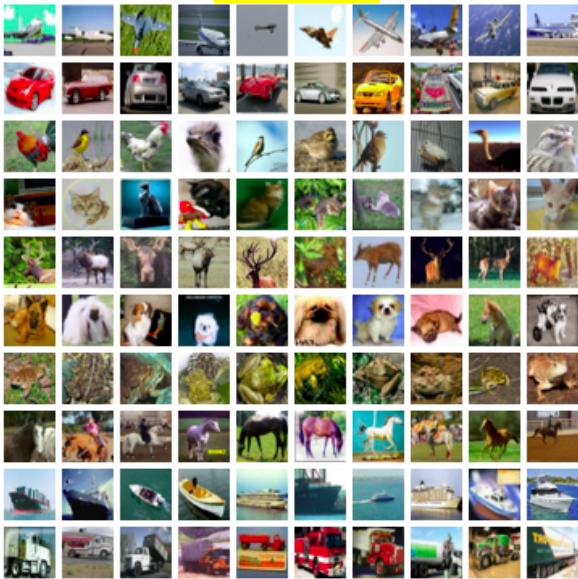
# Convex Optimization

$$W = (w_{131}, w_{132}, \dots)$$



So far ...

$h(w)$



Training  
→  
Optimize  
cost function  
 $h(w)$



Machine  
parameters  
 $w$

# Outline

- Motivation – distributed machine learning
- Research problems
  - Privacy-preserving distributed optimization
  - Adversarial learning
  - Robustness to adversarial samples

# Distributed Machine Learning

- Data is distributed across different agents
  - Mobile users
  - Hospitals
  - Competing vendors



# Distributed Machine Learning

- Data is distributed across different agents

- Mobile users
- Hospitals
- Competing vendors

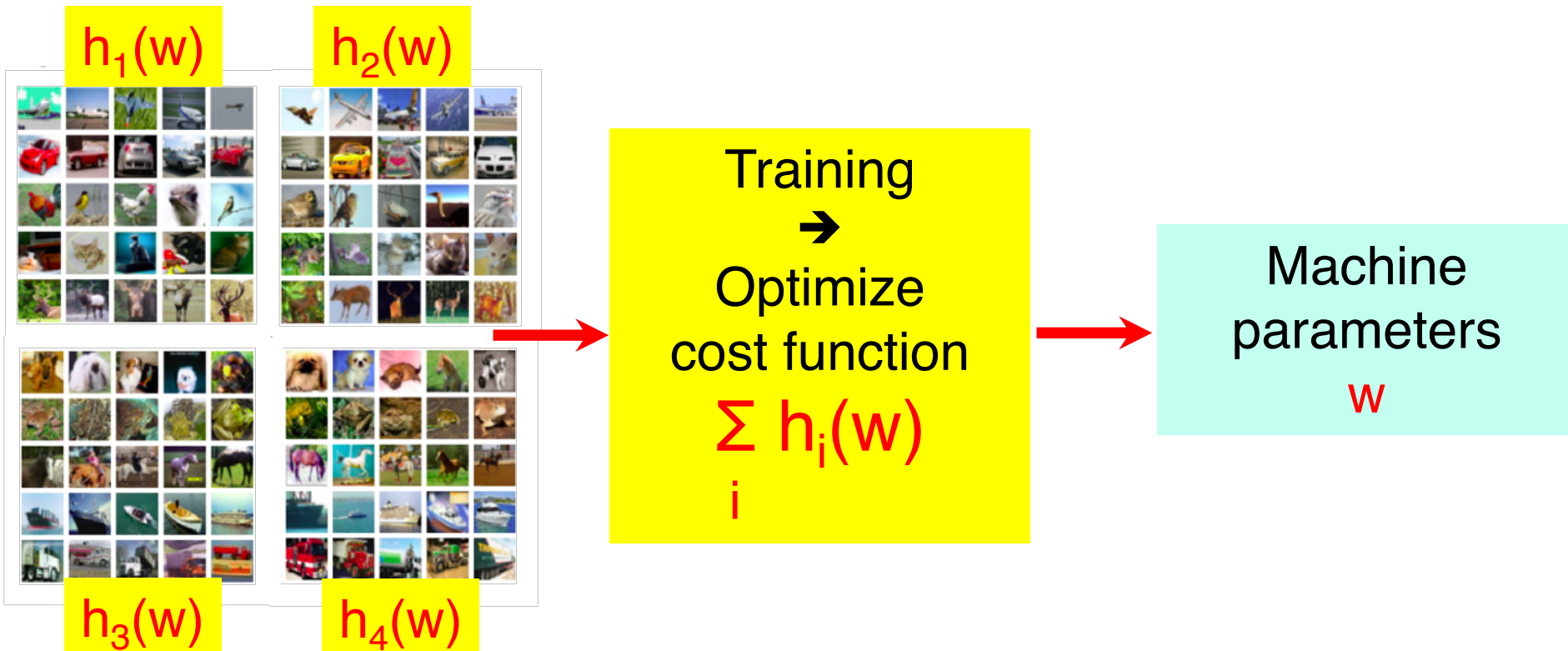


# Distributed Machine Learning

- Data is distributed across different agents → Collaborate to learn

# Distributed Machine Learning

- Data is distributed across different agents → Collaborate to learn



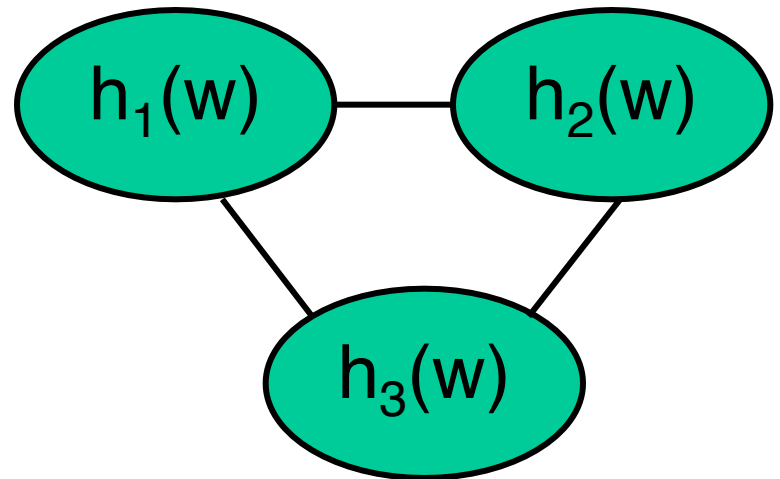
# Distributed Optimization

- 30+ years of work
- Recent interest due to machine learning applications

# Distributed Optimization

Different architectures

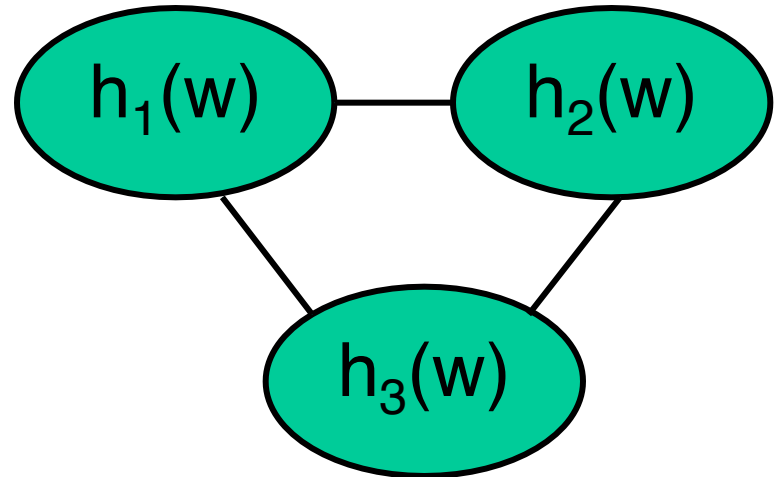
- Peer-to-peer



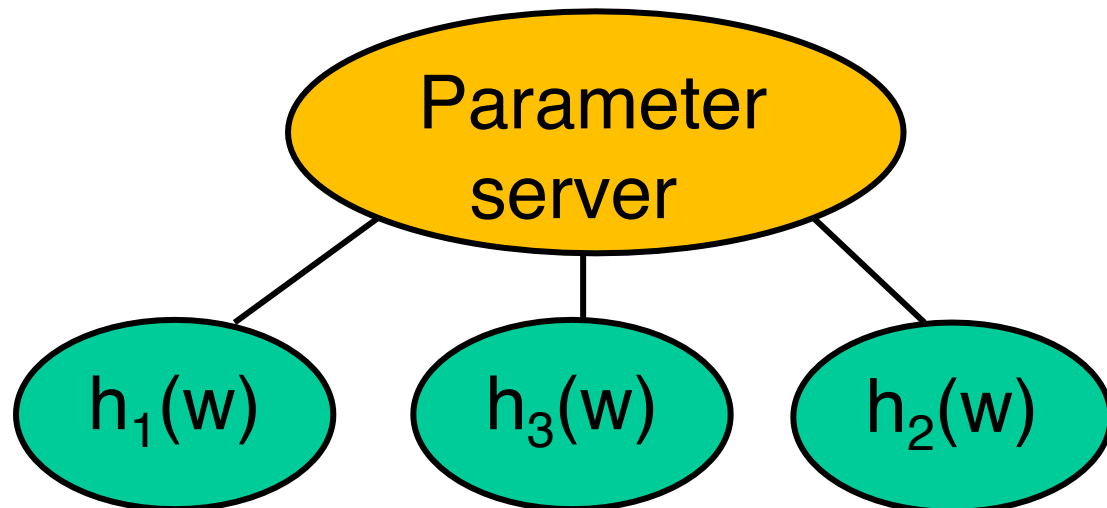
# Distributed Optimization

Different architectures

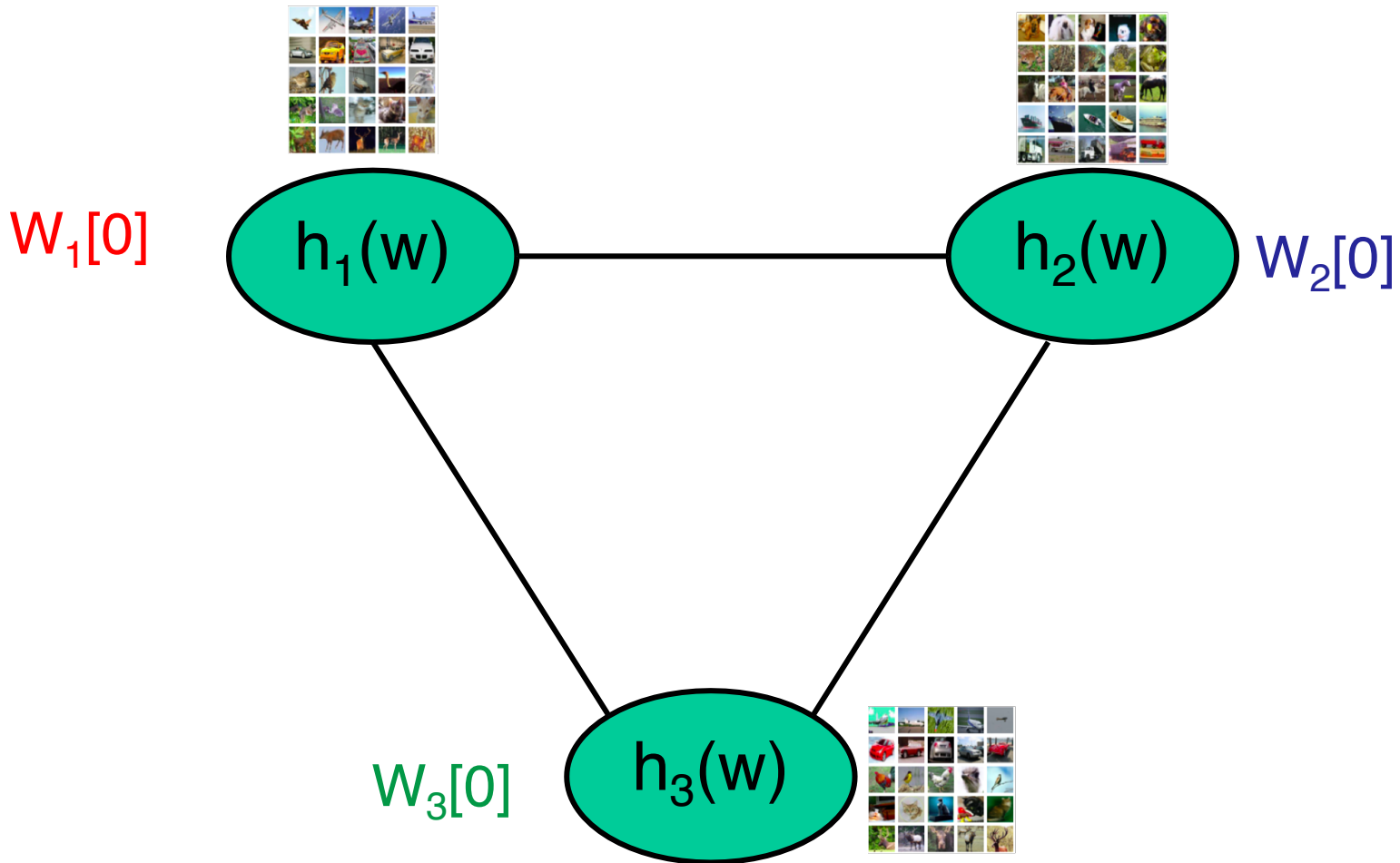
■ Peer-to-peer



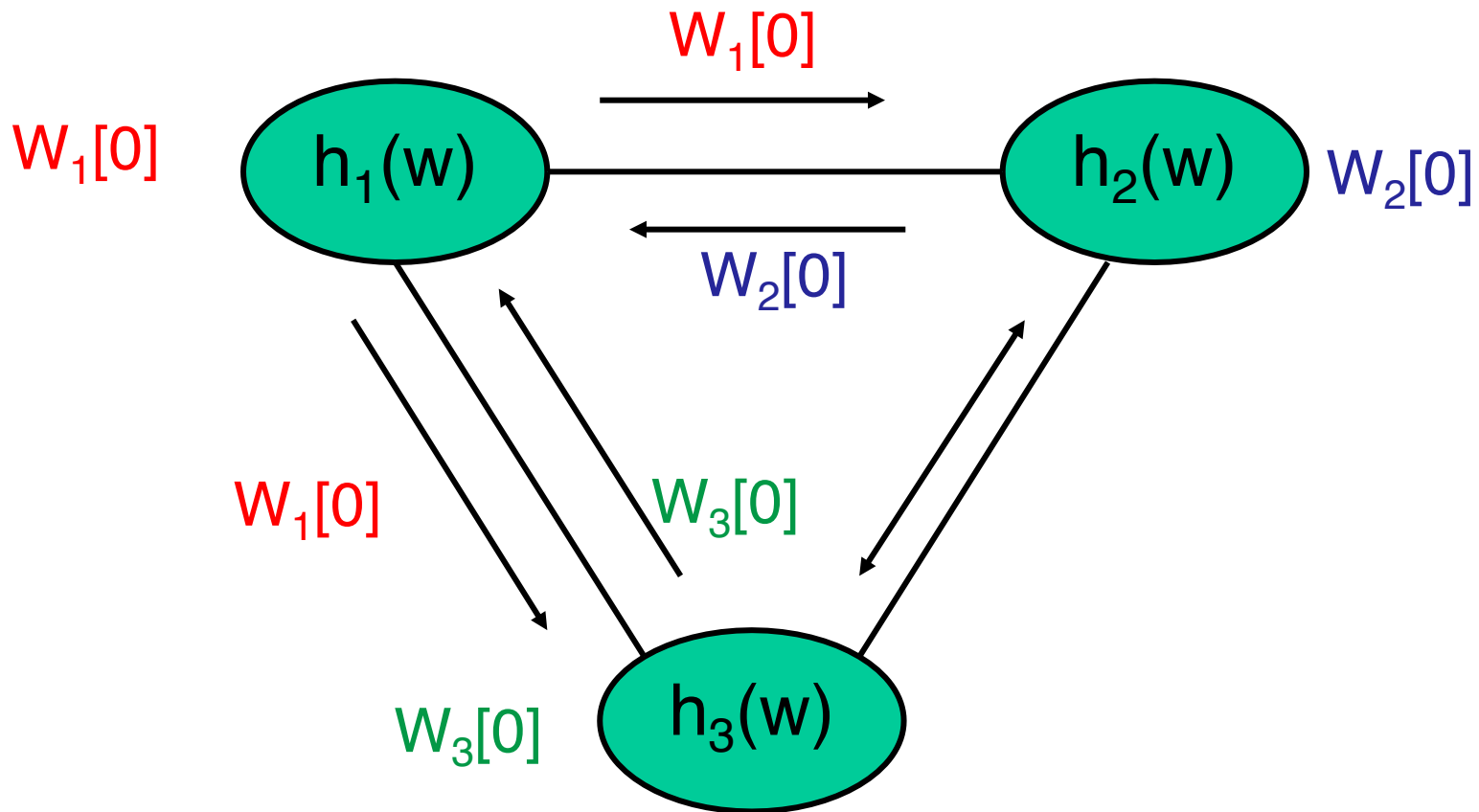
■ Parameter server



# Distributed Gradient Method

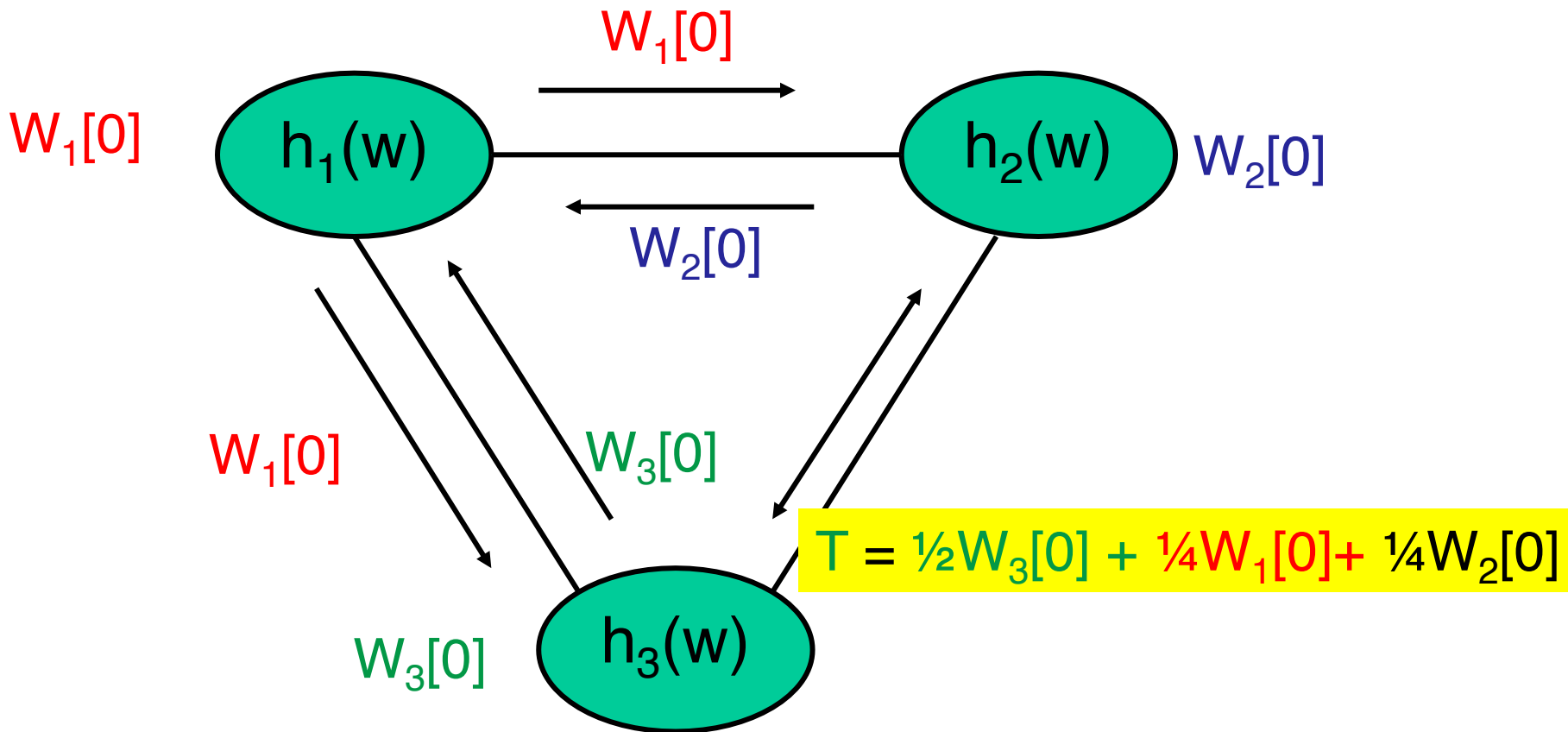


# Distributed Gradient Method

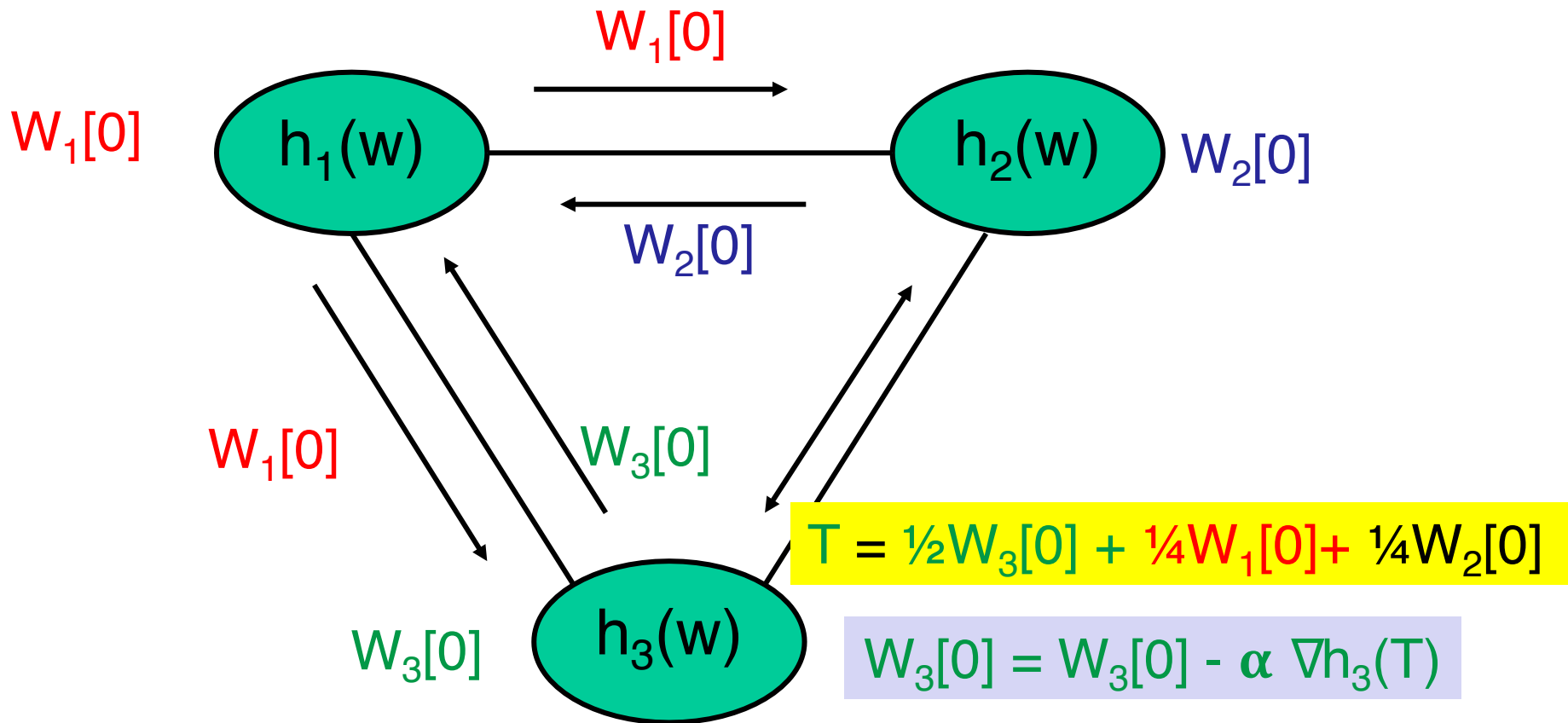




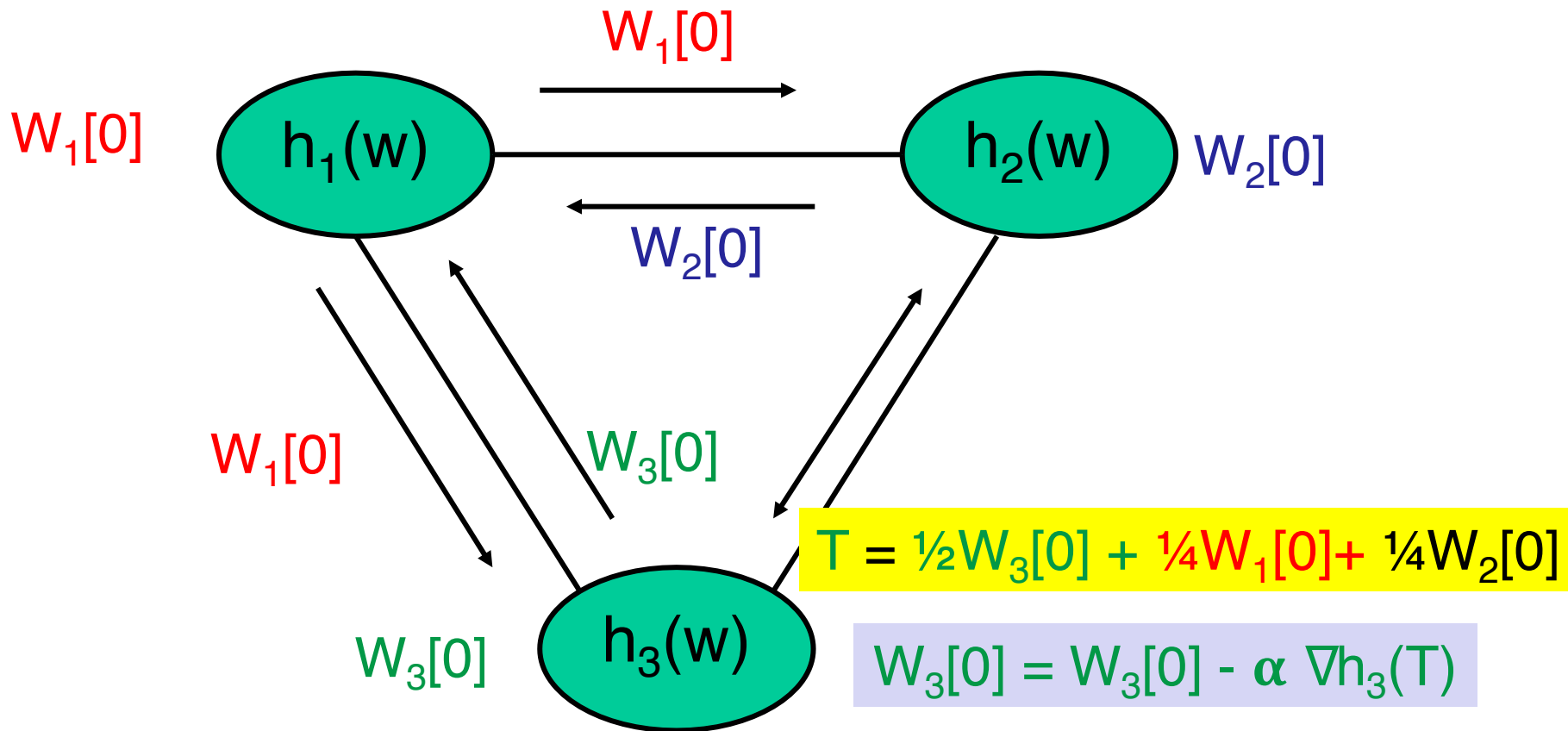
# Distributed Gradient Method



# Distributed Gradient Method

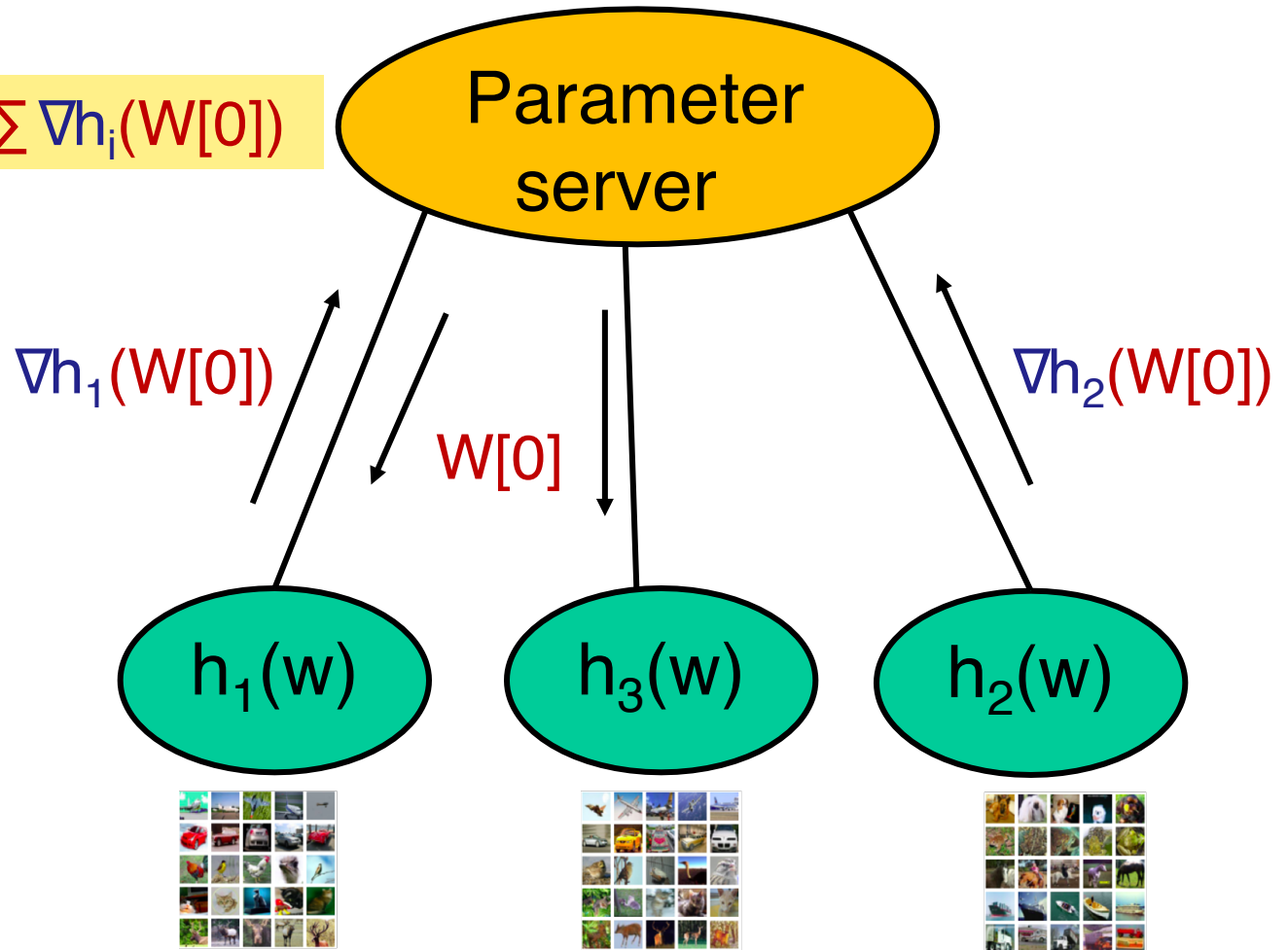


Works in incomplete networks too !!



# Parameter Server Architecture

$$W[1] = W[0] - \alpha \sum \nabla h_i(W[0])$$



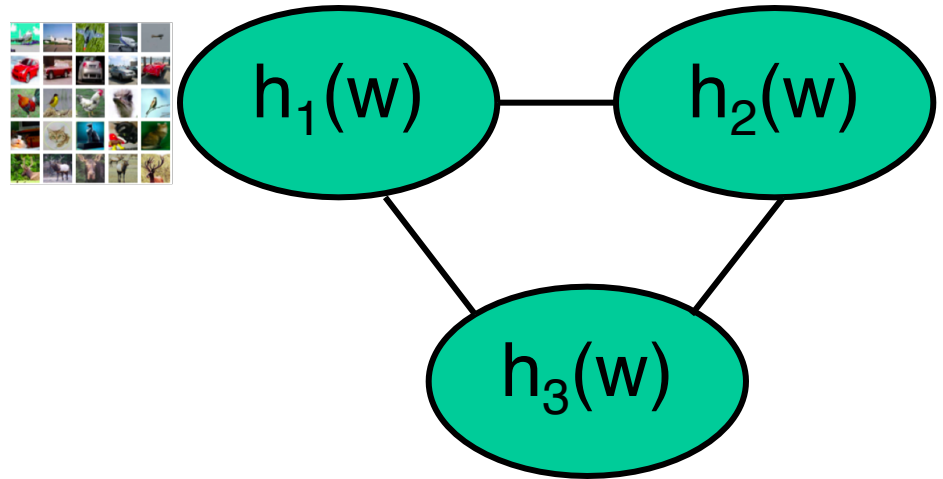


# Outline

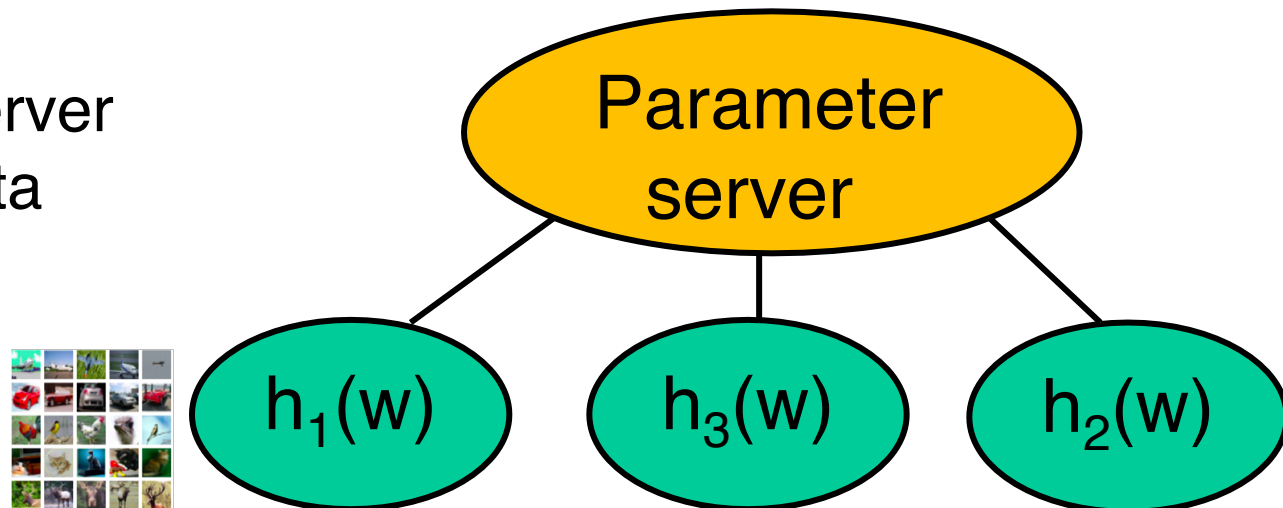
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# Privacy Challenge

- Peers may learn each other's data

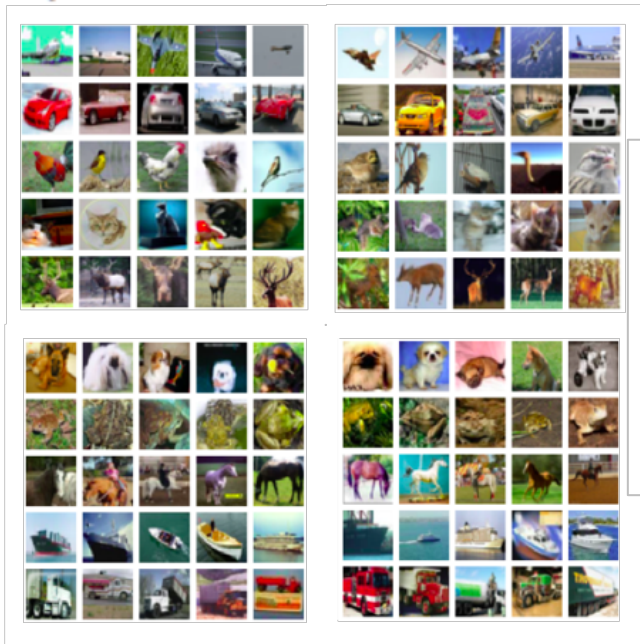


- Parameter server may learn data



# Privacy-Preserving Optimization

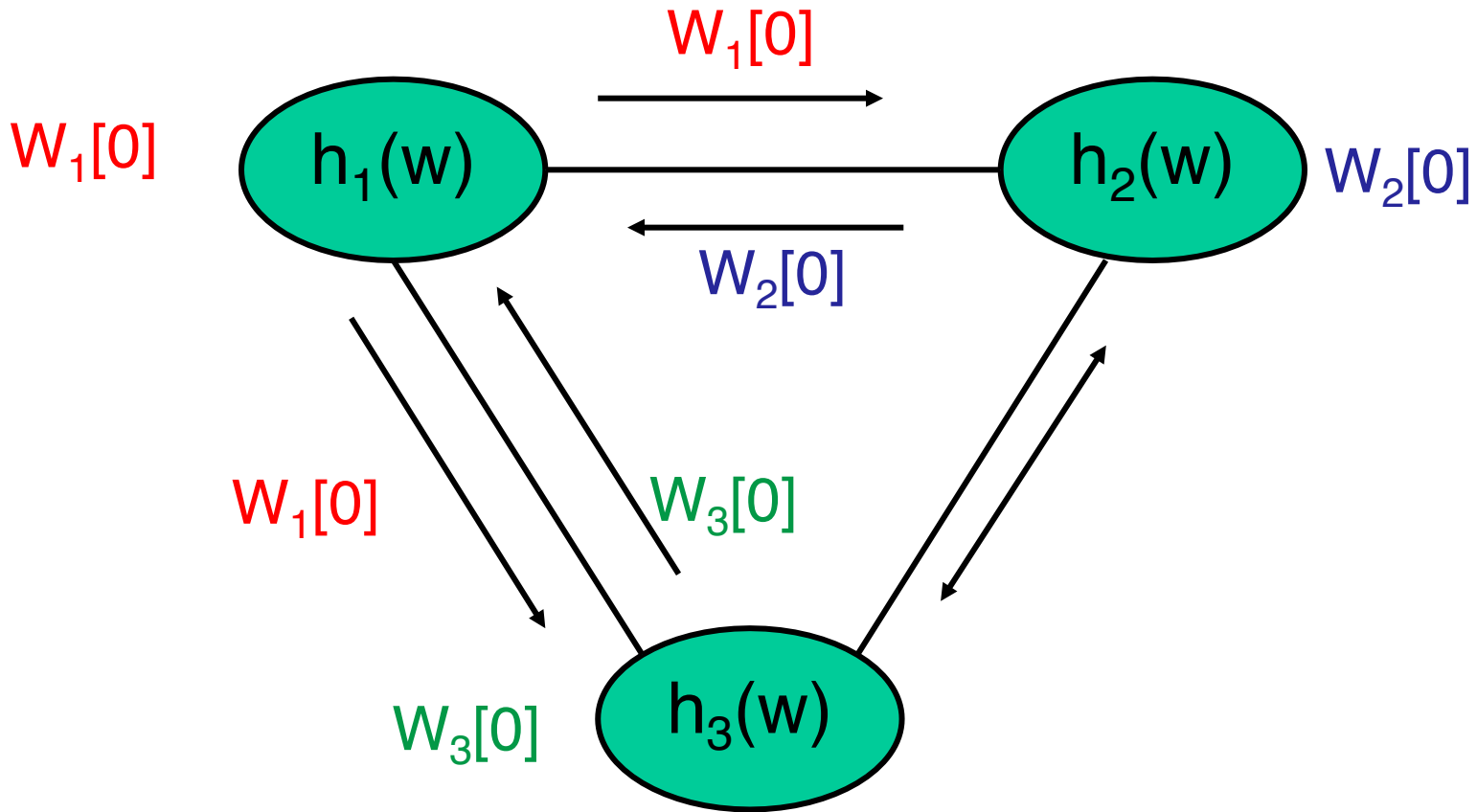
Can agents collaboratively learn,  
and yet protect own data ?



Optimize  
cost function

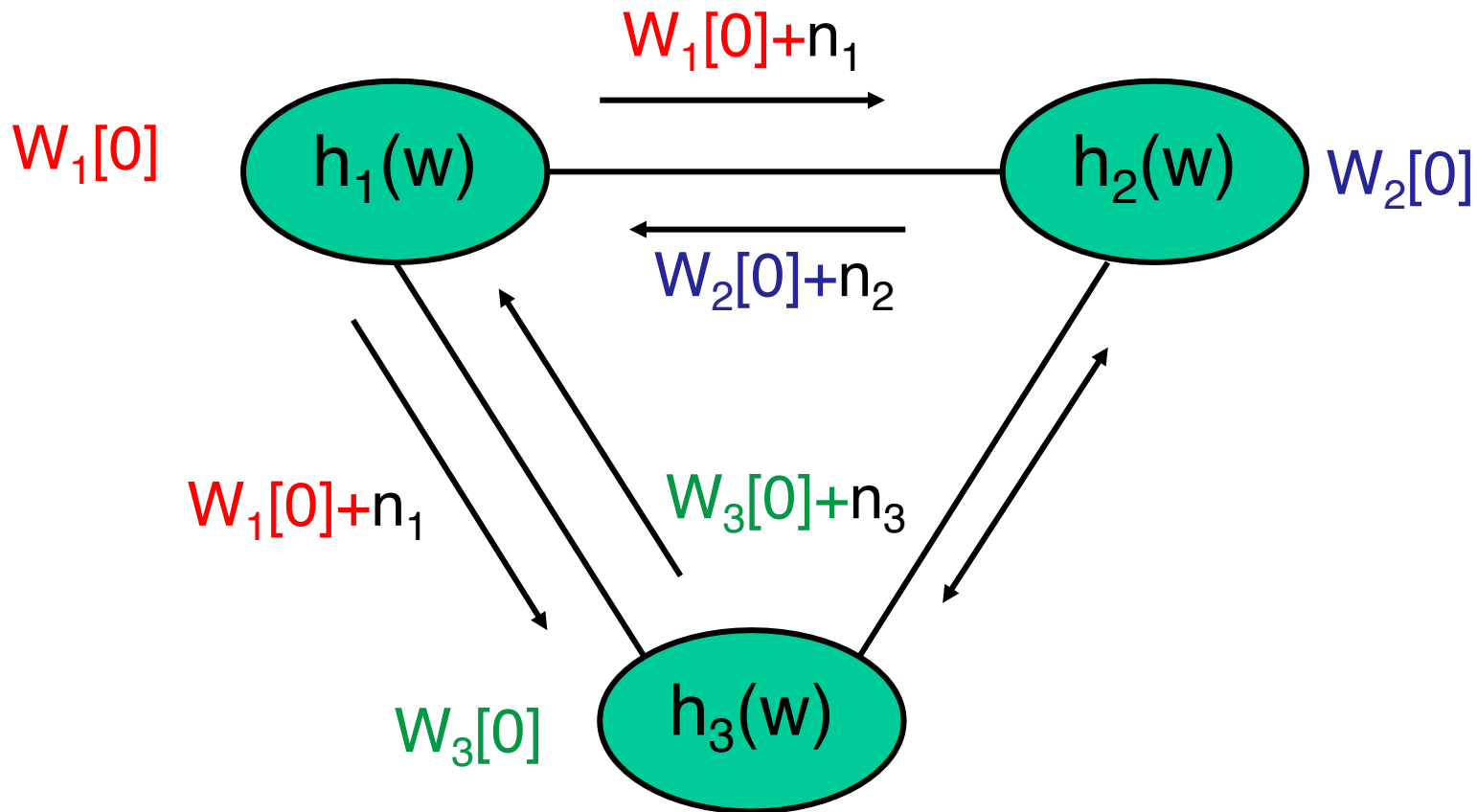
$$\sum_i h_i(w)$$

# Peer-to-Peer Architecture

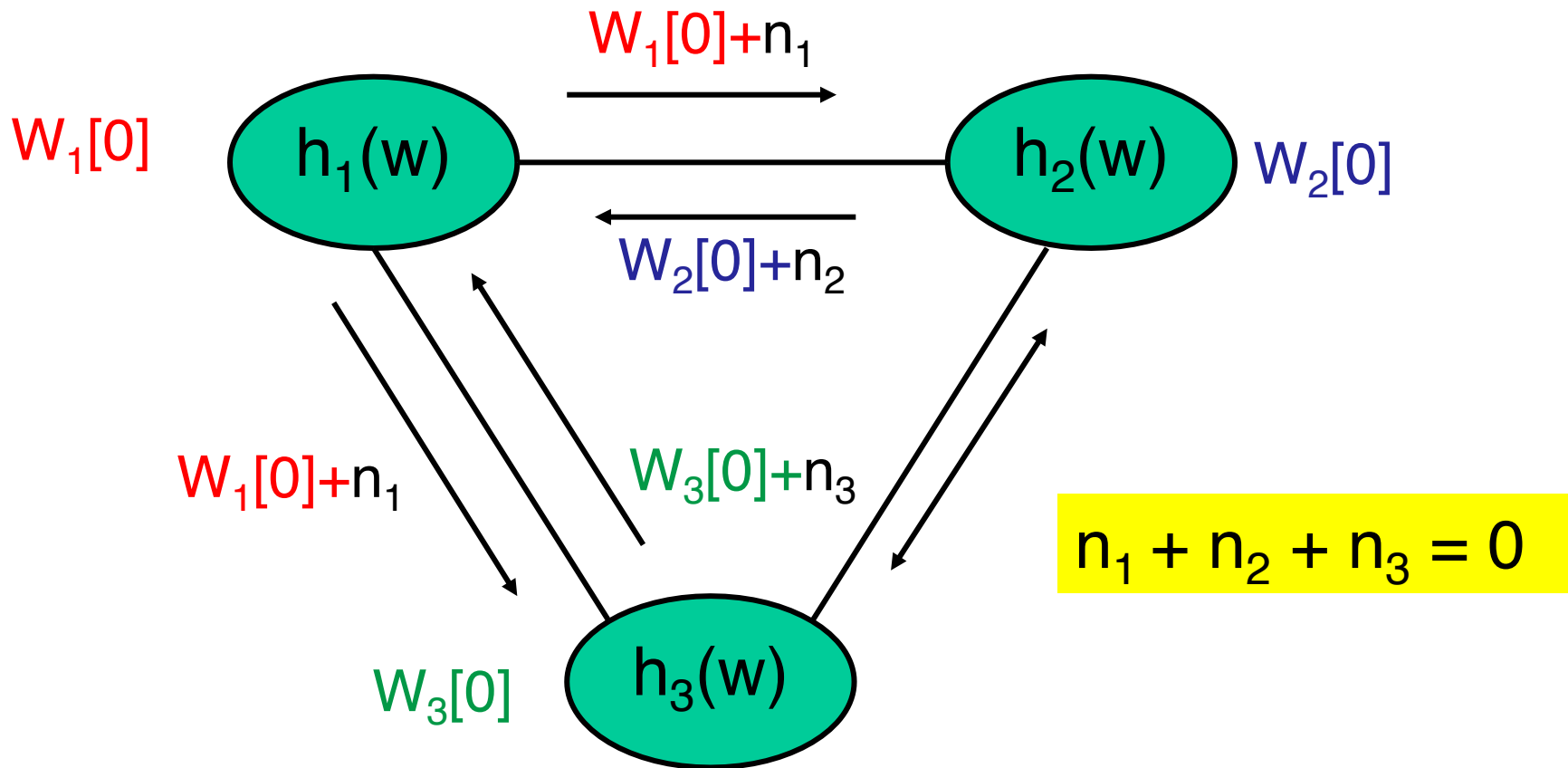




# Add Inter-Dependent Noise



# Add Inter-Dependent Noise

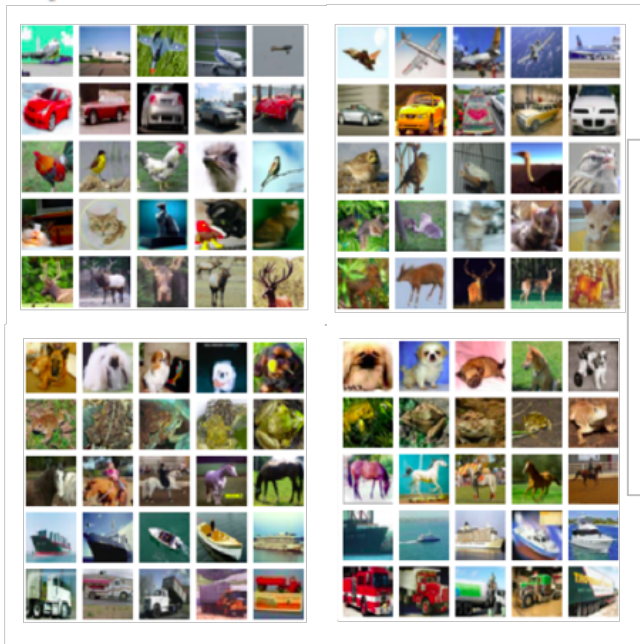


## Key Idea

- Add **correlated noise** in information exchanged between agents
- Noise “**cancel**s” over the network
- But can prevent coalition of bad agents learning information about others

# Privacy-Preserving Optimization

Can agents collaboratively learn,  
and yet protect own data ?



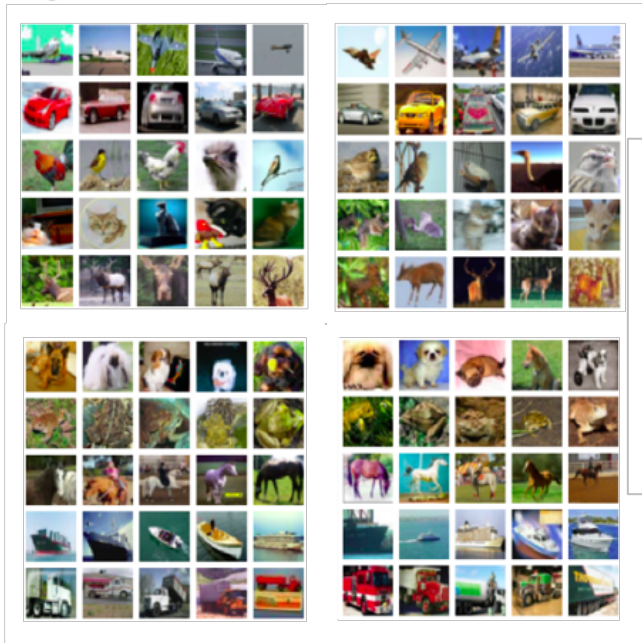
Optimize  
cost function

$$\sum_i h_i(w)$$

**Yes!\***

# Privacy-Preserving Optimization

Can agents collaboratively learn,  
and yet protect own data ?



Optimize  
cost function

$$\sum_i h_i(w)$$

**Yes!**\*

\* conditions  
apply

# Private Learning on Networks \*

Shripad Gade      Nitin H. Vaidya

Department of Electrical and Computer Engineering, and  
Coordinated Science Laboratory,  
University of Illinois at Urbana-Champaign.  
Email: {gade3, nhv}@illinois.edu

Technical Report

## Abstract

Continual data collection and widespread deployment of machine learning algorithms, particularly the distributed variants, have raised new privacy challenges. In a distributed machine learning scenario, the dataset is stored among several machines and they solve a distributed optimization problem to collectively learn the underlying model. We present a secure multi-party computation inspired privacy preserving distributed algorithm for optimizing a convex function consisting of several possibly non-convex functions. Each individual objective function is privately stored with an agent while the agents communicate model parameters with neighbor machines connected in a network. We show that our algorithm can correctly optimize the overall objective function and learn the underlying model accurately. We further prove that under a vertex connectivity condition on the topology, our algorithm preserves privacy of individual objective functions. We establish limits on the what a coalition of adversaries can learn by observing the messages and states shared over a network.

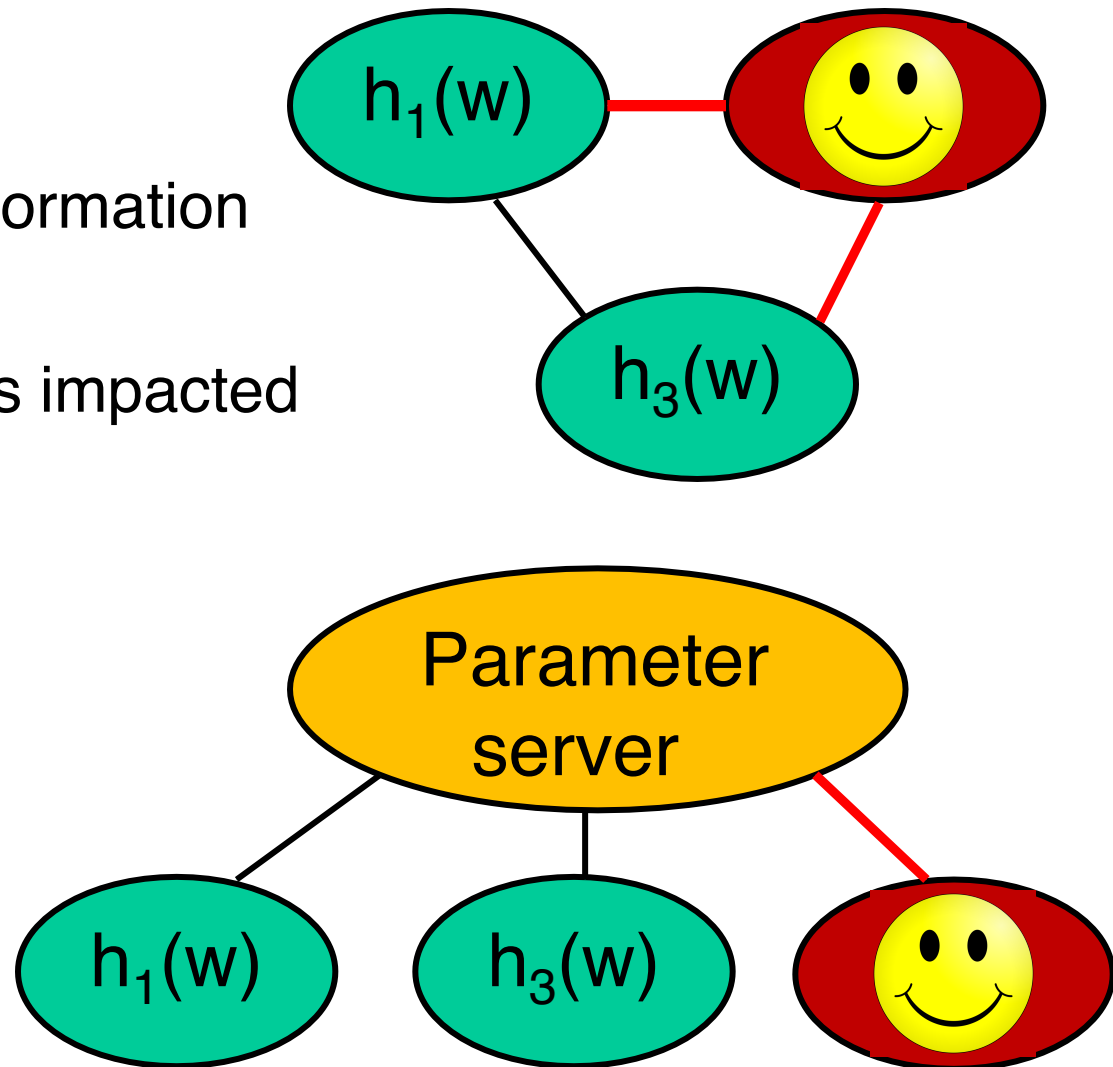


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# Adversarial Agents

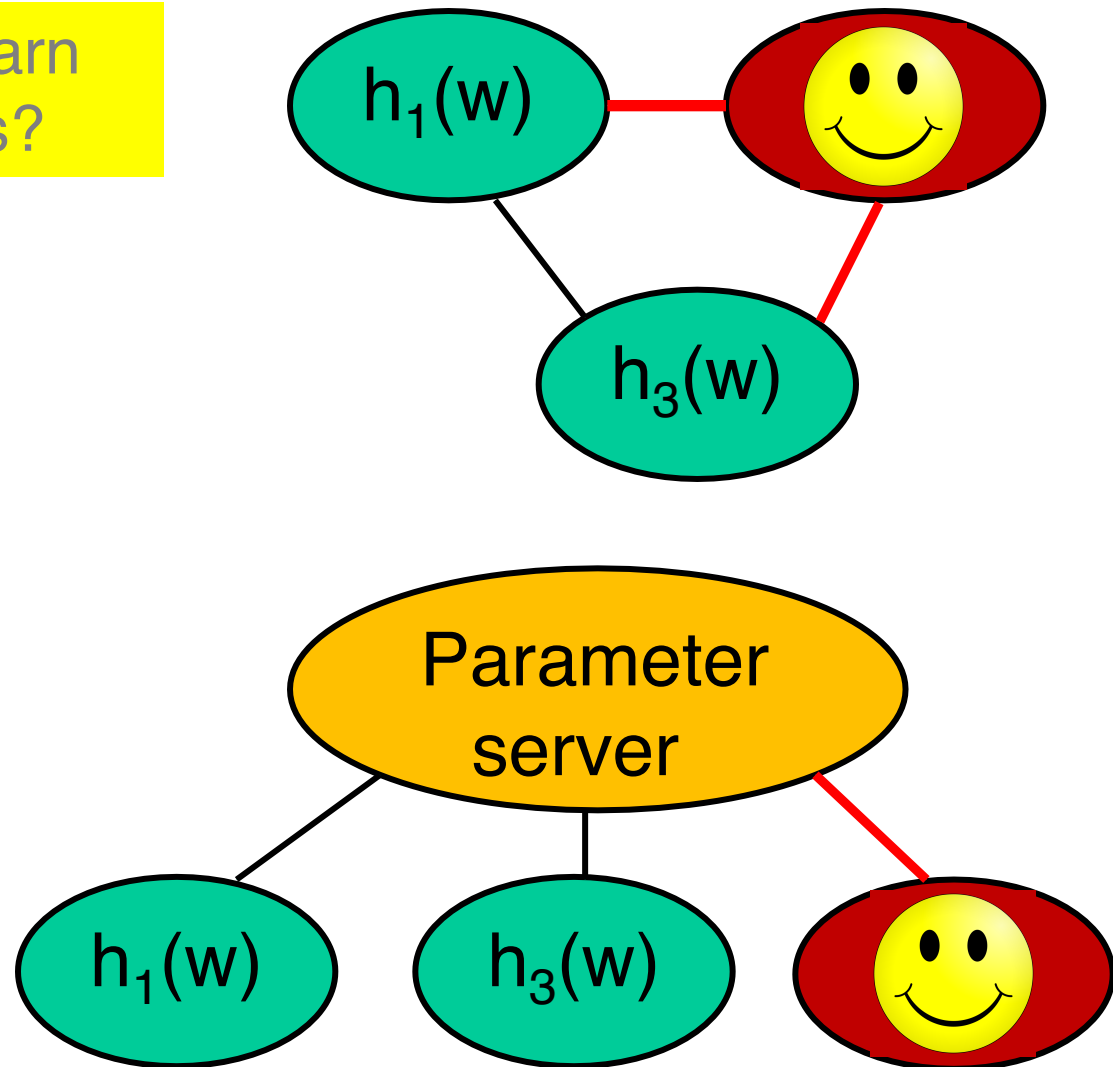
- Adversarial agents may send bogus information
- Learned parameters impacted





# Adversarial Agents

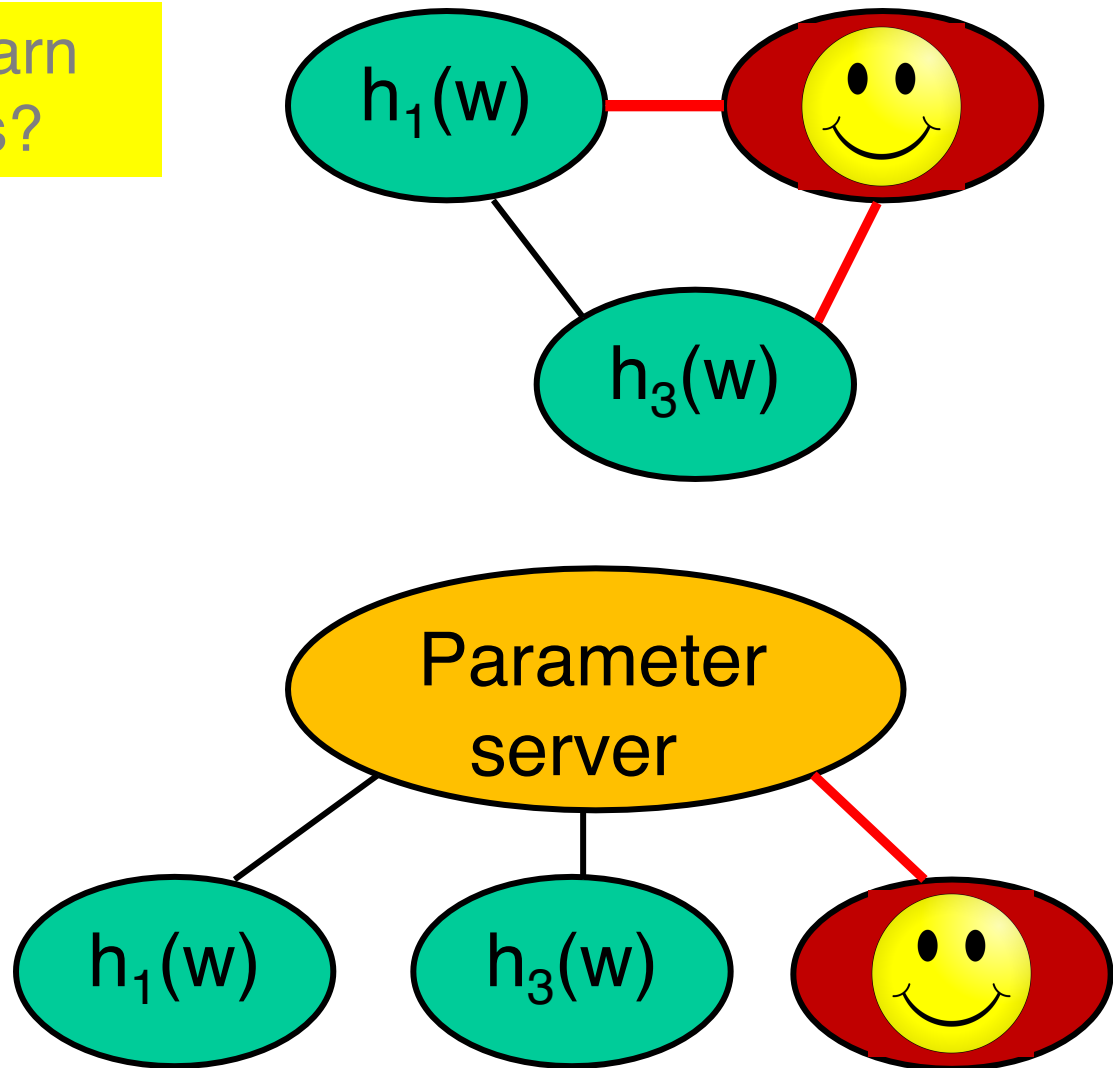
Can good agents learn despite bad agents?



# Adversarial Agents

Can good agents learn despite bad agents?

Yes! \*



## Key Idea

- Need to filter bad information
- Define “outliers” appropriately

# Non-Bayesian Learning in the Presence of Byzantine Agents

Lili Su<sup>(✉)</sup> and Nitin H. Vaidya

Department of Electrical and Computer Engineering,  
University of Illinois at Urbana-Champaign, Champaign, USA  
{lilisu3,nhv}@illinois.edu

**Abstract.** This paper addresses the problem of non-Bayesian learning over multi-agent networks, where agents repeatedly collect partially informative observations about an *unknown* state of the world, and try to collaboratively learn the true state. We focus on the impact of the Byzantine agents on the performance of consensus-based non-Bayesian learning. Our goal is to design an algorithm for the *non-faulty* agents to collaboratively learn the true state through local communication.

We propose an update rule wherein each agent updates its local beliefs as (up to normalization) the product of (1) the likelihood of the *cumulative* private signals and (2) the weighted geometric average of the beliefs of its incoming neighbors and itself (using Byzantine consensus). Under mild assumptions on the underlying network structure and the global identifiability of the network, we show that all the non-faulty agents asymptotically agree on the true state almost surely.

**Keywords:** Distributed learning · Byzantine agreement · Fault-tolerance · Adversary attacks · Security

Boston Marriott Copley Place  
July 6-8, 2016. Boston, MA, USA

# Multi-Agent Optimization in the Presence of Byzantine Adversaries: Fundamental Limits\*

Lili Su and Nitin Vaidya

*Abstract*— We study multi-agent optimization problem in the presence of Byzantine adversaries, where each agent  $i$  has a local cost function  $h_i(x)$ , and some unknown subset of agents suffer Byzantine faults. The goal is to optimize a global objective that properly aggregates the local cost functions. Ideally, we would like to optimize  $\frac{1}{|\mathcal{N}|} \sum_{i \in \mathcal{N}} h_i(x)$ , where  $\mathcal{N}$  is the set of non-faulty agents. However, we show that this ideal goal is unachievable. Therefore, we define a relaxed version of the problem, named Byzantine multi-agent optimization, for which the goal is to generate an output that is an optimum of a global cost function formed as a *convex combination* of local cost functions kept by the non-faulty agents. More precisely, there must exist nonnegative weights  $\alpha_i$  for  $i \in \mathcal{N}$  such that  $\sum_{i \in \mathcal{N}} \alpha_i = 1$ , and the output is an optimum of  $\sum_{i \in \mathcal{N}} \alpha_i h_i(x)$ .

In this paper, we focus on the impact of Byzantine attacks on the maximal achievable number of nonzero weights. To characterize the fundamental limits, we assume that the argument of each local cost function is a (real-valued) scalar, the network is fully-connected, and there is no restriction on the information exchange among agents. We show that the number of nonzero weights ( $\alpha_i$ 's) that can be guaranteed is at most  $|\mathcal{N}| - f$ , where  $f$  is the maximum number of Byzantine faulty agents. Additionally, we present algorithms that achieve this upper bound. By exploiting Byzantine broadcast for information exchange between agents, our proposed algorithms essentially

$$\text{output } x_o \in \underset{x}{\operatorname{argmin}} \frac{1}{n} \sum_{i=1}^n h_i(x) \quad (1)$$

Each function  $h_i(x)$  is assumed to be a *convex* function. (Section III will fully describe the properties of the cost functions.)

Due to its many potential applications, distributed multi-agent optimization has been a topic of significant research activity, as noted above. The applications include distributed machine learning, distributed resource allocation, and distributed robotics. In distributed machine learning problem [1],  $x$  represents parameters that need to be learned, using data available to a collection of agents.  $f_i(x)$  denotes a loss function for agent  $i$  that depends on data available to agent  $i$ . In the resource allocation problem, the argument  $x$  represents allocation of shared resources to the agents, and the local cost functions depends on the *fairness* of the resource allocation. The global objective is to allow the agents to collaboratively agree on the most fair resource allocation. As a simple



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# Adversarial Samples

- Machine learning seems to work well
- If it seems too good to be true ...

# Adversarial Samples

- Several researchers have shown that it is easy to fool a machine



Original



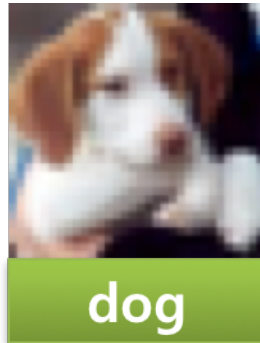
6

Adversarial

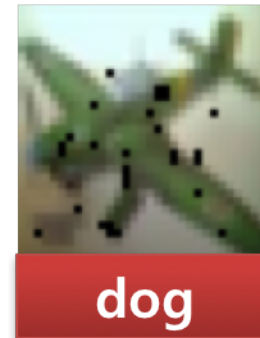
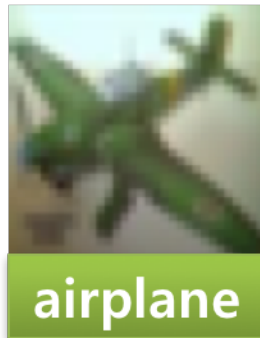
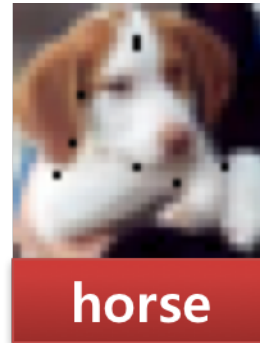


8

original  
sample



adversarial  
sample



# Can we solve the problem?

## May be ... or not

- Some interesting ideas that seem promising in early evaluations

... but not mature enough to report yet



# Summary

- Achieving **privacy/security in learning** is non-trivial
- Some promising progress
- Plenty to keep us busy for a while ...

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# Collaborators

- Lili Su (Ph.D. candidate)
- Shripad Gade (Ph.D. candidate)
- Nishad Phadke (BS thesis)
- Brian Wang (BS thesis)
- Professor Jungmin So (on sabbatical)

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## Other related effort -- fault-tolerant control

- Professor Aranya Chakraborty (on sabbatical)



# Summary

- Achieving privacy/security in **learning** is non-trivial
- Some promising progress
- Plenty to keep us busy for a while ...

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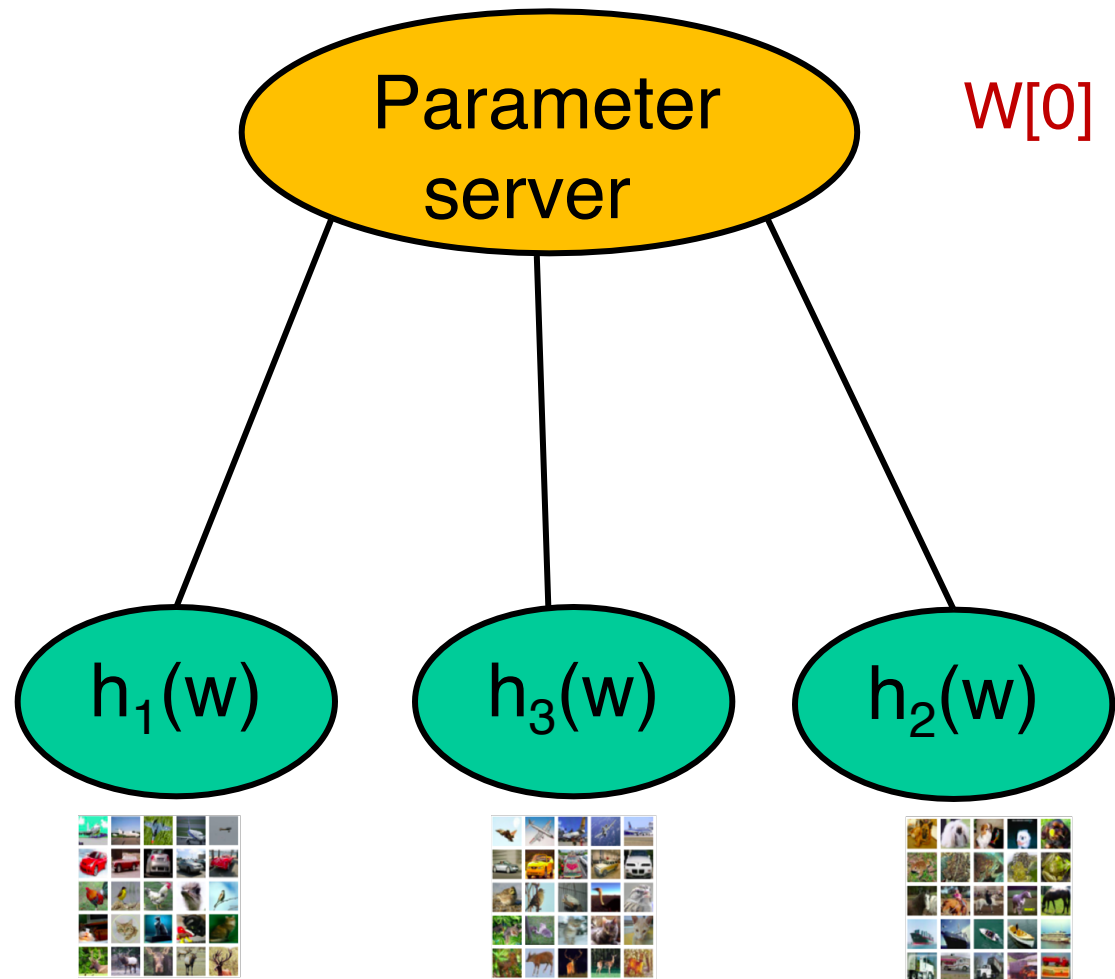




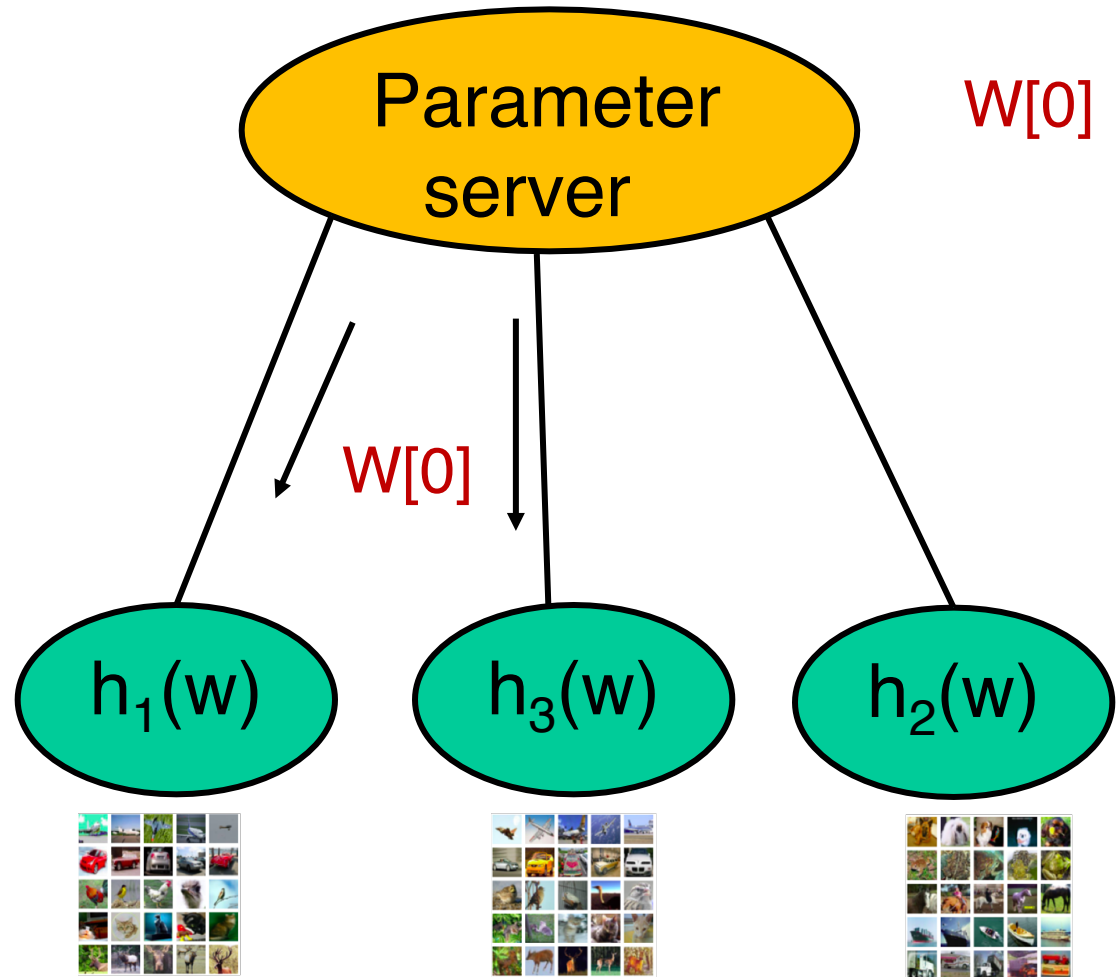


# Parameter Server Architecture

- Distributed gradient method



# Distributed Optimization



# Distributed Optimization

